

ENERGY BALANCE

1) Balance around feed preheater heat exchanger:

The mixed feed, which is assumed to be at around 30°C & have both liquid & vapour phases enters into the heat exchanger & gets heated to a temperature of 200°C by taking heat from the reactor effluent stream, which is at 750°C.

a) Feed stream entering:

$$T = 30^{\circ}\text{C}$$

$$\text{Hydrogen} - 1633.2607 \text{ kmol/hr}$$

$$\text{Methane} - 1156.1750 \text{ kmol/hr}$$

$$\text{Benzene} - 1.0591 \text{ kmol/hr}$$

$$\text{Toluene} - 191.5207 \text{ kmol/hr}$$

Specific heats at 30°C,

$$\text{Hydrogen} - C_{p_{H(g)}} = 29.5 \text{ kJ/kmolK}$$

$$\text{Methane} - C_{p_{M(g)}} = 36.9 \text{ kJ/kmolK}$$

$$\text{Benzene} - C_{p_{B(l)}} = 136 \text{ kJ/kmolK}$$

$$\text{Toluene} - C_{p_{T(l)}} = 156 \text{ kJ/kmolK}$$

b) Reactor effluent stream entering:

$$T = 750^{\circ}\text{C}$$

$$\text{Hydrogen} - 1499.1962 \text{ kmol/hr}$$

$$\text{Methane} - 1290.2397 \text{ kmol/hr}$$

$$\text{Benzene} - 135.1314 \text{ kmol/hr}$$

$$\text{Toluene} - 57.4562 \text{ kmol/hr}$$

Specific heats at 750°C,

$$\text{Hydrogen} - C_{p_{H(g)}} = 29.5 \text{ kJ/kmolK}$$

$$\text{Methane} - C_{p_{M(g)}} = 73.75 \text{ kJ/kmolK}$$

$$\text{Benzene} - C_{p_{B(g)}} = 215 \text{ kJ/kmolK}$$

$$\text{Toluene} - C_{p_{T(g)}} = 265 \text{ kJ/kmolK}$$

c) Feed stream leaving:

$$T = 200^{\circ}\text{C}$$

$$\text{Hydrogen } -C_{p_{H(g)}} = 29.5 \text{ kJ/kmolK}$$

$$\text{Methane } -C_{p_{M(g)}} = 45.5 \text{ kJ/kmolK}$$

$$\text{Benzene } -C_{p_{B(g)}} = 135 \text{ kJ/kmolK}$$

$$\text{Toluene } -C_{p_{T(g)}} = 165 \text{ kJ/kmolK}$$

Boiling point of benzene = 80.1°C ,

Latent heat of vaporisation, $\lambda_B = 94.14 \text{ cal/g} = 30736.7 \text{ kJ/kmol}$

Boiling point of toluene = 110.62°C ,

Latent heat of vaporisation, $\lambda_T = 86.8 \text{ cal/g} = 33426.98 \text{ kJ/kmol}$

Balance gives,

$$\begin{aligned} &1633.2607 \times 29.5 \times (200-30) + 1156.1750 \times 36.9 \times (200-30) + \\ &1.0591 \times [136 \times (80.1-30) + 30736.7 + 135 \times (200-80.1)] + \\ &191.5207 \times [156 \times (110.62-30) + 33426.98 + 165 \times (200-110.62)] = [1499.1962 \times 29.5 \\ &+ 1290.2397 \times 73.75 + 135.1314 \times 215 + 57.4562 \times 265] (750-T) \end{aligned}$$

$$T = \underline{602^{\circ}\text{C}}.$$

2) Balance around heater:

In the heater, the feed stream is heated to the reaction temperature, ie, 750°C .

The average specific heats taken are,

$$\text{Hydrogen } -C_{p_{H(g)}} = 29.5 \text{ kJ/kmolK}$$

$$\text{Methane } -C_{p_{M(g)}} = 60 \text{ kJ/kmolK}$$

$$\text{Benzene } -C_{p_{B(g)}} = 175 \text{ kJ/kmolK}$$

$$\text{Toluene } -C_{p_{T(g)}} = 215 \text{ kJ/kmolK}$$

$$\begin{aligned} \text{The heat to be supplied in the reactor} &= (1633.2607 \times 29.5 + 1156.1750 \times 60 + \\ & 1.0591 \times 175 + 191.5207 \times 215) (750-200) \\ &= \underline{8.74 \times 10^7 \text{ kJ/hr}} \end{aligned}$$

3) Balance around reactor:

In the reactor, exothermic reaction is undergoing & hence some mechanism to remove the heat generated such as quenching or cooling water circulation in shell has to be done to maintain the reactor in isothermal conditions.

Heat of formation of different components are given below.

$$\text{Hydrogen} - H^f = 82930 + 215 \times (750-25) = 238805 \text{ kJ/kmol}$$

$$\text{Methane} - H^f = 50170 + 265 \times (750-25) = 242295 \text{ kJ/kmol}$$

$$\text{Benzene} - H^f = 74520 + 73.75 \times (750-25) = 21051.25 \text{ kJ/kmol}$$

$$\text{Toluene} - H^f = 0 + 29.5 \times (750-25) = 21387.5 \text{ kJ/kmol}$$

$$\begin{aligned} \text{Heat of reaction, } \Delta H^R &= \Sigma H^f, \text{ products} - \Sigma H^f, \text{ reactants} \\ &= (238805 - 21051.25) - (242295 + 21387.5) \\ &= \underline{-4.59 \times 10^4 \text{ kJ/kmol}} \end{aligned}$$

$$\begin{aligned} \text{Number of kmoles reacting per hour} &= 191.5207 - 57.4562 \\ &= 134.0645 \text{ kmoles} \end{aligned}$$

$$\begin{aligned} \text{Therefore, heat to be removed from the reactor per hour} &= 134.0645 \times 4.59 \times 10^4 \text{ kJ} \\ &= \underline{6.16 \times 10^6 \text{ kJ}} \end{aligned}$$

4) Heat exchanger cooling reactor effluents:

The effluent stream from the reactor, after heating the feed has to be further cooled to ambient temperature, say 45°C using water at 30°C. The temperature of effluent stream is 602°C & water is heated to 40°C.

The balance gives,

$$\begin{aligned} & 1499.1962 \times 29.5 \times (602-45) + 1290.2397 \times 60 \times (602-45) + 135.1314 \times [175(602-80.1) \\ & + 30736.7 + 136(80.1-45)] + 57.4562 \times [215(602-110.62) + 33426.98 + 156(110.62-45)] \\ & = M (4.187 \times 18)(40-30) \end{aligned}$$

$$M = 620.13 \text{ kg/s.}$$

Hence use of multiple heat exchangers will be more suitable.

5) Balance around condenser:

$$T = 81^\circ\text{C}$$

$$\text{Latent heat of vaporisation, } \lambda_B = 94.14 \text{ cal/g} = 30736.7 \text{ kJ/kmol}$$

$$\text{Latent heat of vaporisation, } \lambda_T = 86.8 \text{ cal/g} = 33426.98 \text{ kJ/kmol}$$

$$\text{Benzene} - 133.4 \text{ kmol/hr}$$

$$\text{Toluene} - 5.5583 \text{ kmol/hr}$$

$$\text{Heat duty} = 133.4 \times 30736.7 + 5.5583 \times 33426.98 = \underline{4.29 \times 10^6 \text{ kJ/hr.}}$$

6) Balance around reboiler:

$$T = 110^\circ\text{C}$$

$$\text{Benzene} - 1.0591 \text{ kmol/hr}$$

$$\text{Toluene} - 51.8979 \text{ kmol/hr}$$

$$\text{Heat duty} = 1.0591 \times 30736.7 + 51.8979 \times 33426.98 = \underline{1.77 \times 10^6 \text{ kJ/kmol}}$$