

5.1 PROCESS DESIGN OF DISTILLATION COLUMN:

5.1.1 Glossary of notations used:

F = molar flow rate of Feed, kmol/hr.

D = molar flow rate of Distillate, kmol/hr.

W = molar flow rate of Residue, kmol/hr.

x_F = mole fraction of Acetaldehyde in liquid/Feed.

y_D = mole fraction of Acetaldehyde in Distillate.

x_W = mole fraction of Acetaldehyde in Residue.

M_F = Average Molecular weight of Feed, kg/kmol

M_D = Average Molecular weight of Distillate, kg/kmol

M_W = Average Molecular weight of Residue, kg/kmol

R_m = Minimum Reflux ratio

R = Actual Reflux ratio

L = Molar flow rate of Liquid in the Enriching Section, kmol/hr.

G = Molar flow rate of Vapor in the Enriching Section, kmol/hr.

\bar{L} = Molar flow rate of Liquid in Stripping Section, kmol/hr.

\bar{G} = Molar flow rate of Vapor in Stripping Section, kmol/hr.

q = Thermal condition of Feed

ρ_L = Density of Liquid, kg/m³.

ρ_V = Density of Vapor, kg/m³.

q_L = Volumetric flow rate of Liquid, m³/s

q_V = Volumetric flow rate of Vapor, m³/s

μ_L = Viscosity of Liquid, cP.

T_L = Temperature of Liquid, °K.

T_V = Temperature of Vapor, °K

T – x- y data:

T⁰C	98.5	89.9	80	71	60.5	50	39
X	0.000	0.069	0.164	0.286	0.445	0.664	1.000
Y	0.000	0.317	0.578	0.761	0.879	0.954	1.000

Table 5.1 T-x-y data.

5.1.2 Preliminary calculations:

$$F = 152.798 \text{ kmol/hr}, x_F = 0.938, M_F = 44.123 \text{ kg/kmol.}$$

$$D = 144.7 \text{ kmol/hr}, x_D = 0.99, M_D = 44.04 \text{ kg/kmol.}$$

$$W = 8.0931 \text{ kmol/hr}, x_W = 0.177, M_W = 45.64 \text{ kg/kmol.}$$

Distillation column temperature = 40⁰ C.

Distillation column pressure = 2.08 atm. = 1586.41 mm Hg.

Basis: One-hour operation.

From the graph,

$$x_D / (R_m + 1) = 0.94$$

$$\text{Thus, } R_m = 0.0476$$

$$\text{Let, } R = 1.5 * R_m$$

$$\text{Therefore, } R = 1.5 * 0.0476 = 0.0714$$

$$\text{Thus, } x_D / (R + 1) = 0.99 / (0.0714 + 1)$$

$$\text{i.e., } x_D / (R + 1) = 0.924$$

Number of Ideal trays = 4 (including the reboiler).

Reboiler is the last tray.

Number of Ideal trays in Enriching Section = 2

Number of Ideal trays in Stripping Section = 2

Now, we know that,

$$R = L_o / D$$

$$\Rightarrow L_o = R * D$$

$$\text{i.e., } L_o = 0.0714 * 144.7$$

$$\text{i.e., } L_o = 10.33 \text{ kmol/hr.}$$

Therefore, $L_o = 10.33 \text{ kmol/hr.}$

$$L = \text{Liquid flow rate on the Top tray} = 10.33 \text{ kmol/hr.}$$

Since feed is Liquid, entering at bubble point,

$$q = (H_V - H_F) / (H_V - H_L) = 1$$

Now,

$$\begin{aligned} \text{Slope of } q\text{-line} &= q / (q-1) \\ &= 1 / (1-1) = 1/0 = \infty \end{aligned}$$

Now we know that,

$$\begin{aligned} \overline{(\underline{L} - L)} &= q = 1 \\ \overline{L} &= F + L \\ \text{i.e., } \overline{L} &= 10.33 + 152.798 \\ \text{i.e., } \overline{L} &= 163.128 \text{ kmol/hr.} \end{aligned}$$

Therefore, liquid flow rate in the Stripping Section = 163.128 kmol/hr.

Also, we know that,

$$\begin{aligned} \overline{G} &= [(q-1) \times F] + G \\ \text{i.e., } \overline{G} &= [(1-1) \times F] + G \\ \text{i.e., } \overline{G} &= [0 \times F] + G \\ \text{i.e., } \overline{G} &= 0 + G \\ \overline{G} &= G \end{aligned}$$

Now, we know that,

$$\begin{aligned} G &= L + D \\ \text{i.e., } G &= L_o + D \\ \text{i.e., } G &= 10.33 + 144.7 \\ \text{i.e., } G &= 155.03 \text{ kmol/hr.} \end{aligned}$$

Thus, the flow rate of Vapor in the Enriching Section = 155.03 kmol/hr.

$$\begin{aligned} \text{Since } \overline{G} &= G \\ \overline{G} &= G = 155.03 \text{ kmol/hr.} \end{aligned}$$

Therefore, the flow rate of Vapor in the Stripping Section = 155.03 kmol/hr.

5.1.3 List of parameters used in calculation:

SECTION	ENRICHING SECTION		STRIPPING SECTION		
	PROPERTY	TOP	BOTTOM	TOP	BOTTOM
X		0.99	0.95	0.95	0.177
Y		0.99	0.97	0.97	0.177
Liquid, kmol/hr.	L	10.33	10.33	163.128	163.128
Vapor, kmol/hr.	G	155.03	155.03	155.03	155.03
$T_{\text{liquid}}, ^\circ\text{C}$		39.07	39.77	39.77	80.05
$T_{\text{vapor}}, ^\circ\text{C}$		53.00	54.01	54.01	94.13
$M_{\text{avg.}}$ liquid kg/kmol		44.02	44.1	44.1	45.646
$M_{\text{avg.}}$ Vapor kmol/hr		44.02	44.06	44.06	45.646
Liquid, L kg/hr.		454.726	455.55	7193,9	7446.14
Vapor, G kg/hr		6824.42	6830.02	6830.6	7076.5
Density, ρ_l kg/m ³		784.69	784.50	784.50	747.87
Density, ρ_g kg/m ³		3.4376	3.425	3.425	3.361
$(L/G) (\rho_g / \rho_l)^{0.5}$		0.0039	0.004	0.06958	0.0705

Table 5.2 Parameters used in calculations.

5.1.4 Design Specification:

a) Design of Enriching Section:

Tray Hydraulics,

The design of a sieve plate tower is described below. The equations and correlations are borrowed from the 6th and 7th editions of Perry's Chemical Engineers' Handbook.

1. Tray Spacing, (t_s):

Let $t_s = 18'' = 457$ mm. (range 0.15 – 1.0 m).

2. Hole Diameter, (d_h):

Let $d_h = 5$ mm. (range 2.5 – 12 mm).

3. Hole Pitch (l_p):

Let $l_p = 3 * d_h$ (range 2.5 to 4.0 times d_h).

i.e., $l_p = 3 * 5 = 15$ mm.

4. Tray thickness (t_T):

Let $t_T = 0.6 * d_h$ (range 0.4 to 0.7 times d_h).

i.e., $t_T = 0.6 * 5 = 3$ mm.

5. Ratio of hole area to perforated area (A_h/A_p):

Refer fig 3

Now, for a triangular pitch, we know that,

Ratio of hole area to perforated area (A_h/A_p) = $\frac{1}{2} (\pi/4 * d_h^2) / [(\sqrt{3}/4) * l_p^2]$

$$\text{i.e., } (A_h/A_p) = 0.90 * (d_h/l_p)^2$$

$$\text{i.e., } (A_h/A_p) = 0.90 * (5/15)^2$$

$$\text{i.e., } (A_h/A_p) = 0.1$$

Thus,

$$(A_h/A_p) = 0.1$$

6. Plate Diameter (D_c):

The plate diameter is calculated based on entrainment flooding considerations

$$L/G \{ \rho_g / \rho_l \}^{0.5} = 0.004 \quad \text{----- (maximum value)}$$

Now for,

$$L/G \{ \rho_g / \rho_l \}^{0.5} = 0.004 \text{ and for a tray spacing of 500 mm.}$$

We have,

From the flooding curve, ----- (fig.18.10, page 18.7, 6th edition Perry.)

Flooding parameter, $C_{sb, flood} = 0.29$ ft/s .

Now,

$$U_{nf} = C_{sb, flood} * (\sigma / 20)^{0.2} [(\rho_l - \rho_g) / \rho_g]^{0.5}$$

---- {eqⁿ. 18.2, page 18.6, 6th edition Perry.}

Where,

U_{nf} = gas velocity through the net area at flood, m/s (ft/s)

$C_{sb, flood}$ = capacity parameter, m/s (ft/s, as in fig.18.10)

σ = liquid surface tension, mN/m (dyne/cm.)

ρ_l = liquid density, kg/m³ (lb/ft³)

ρ_g = gas density, kg/m³ (lb/ft³)

Now, we have,

$$\sigma = 19.325 \text{ mN/m} = 19.325 \text{ dyne/cm.}$$

$$\rho_l = 784.5 \text{ kg/m}^3.$$

$$\rho_g = 3.425 \text{ kg/m}^3.$$

Therefore,

$$U_{nf} = 0.29 * (19.325/20)^{0.2} * [(784.50 - 3.4250) / 3.4250]^{0.5}$$

$$\text{i.e., } U_{nf} = 4.349 \text{ ft/s} = 1.325 \text{ m/s.}$$

Let,

$$\text{Actual velocity, } U_n = 0.8 * U_{nf}$$

$$\text{i.e., } U_n = 0.8 * 1.325$$

$$\text{i.e., } U_n = 1.06 \text{ m/s}$$

It is desired to design with volumetric flow rate maximum (therefore, actual is less than the maximum).

Volumetric flow rate of Vapor at the bottom of the Enriching Section

$$= q_o = 6830.62 / (3600 * 3.4250) = 0.554 \text{ m}^3/\text{s.}$$

Now,

Net area available for gas flow (A_n)

Net area = (Column cross sectional area) - (Down comer area.)

$$A_n = A_c - A_d$$

Thus,

$$\text{Net Active area, } A_n = t_o / U_n = 0.554 / 1.06 = 0.522 \text{ m}^2.$$

$$\text{Let } L_w / D_c = \underline{0.77} \text{ (range 0.6 to 0.85 times } D_c \text{).}$$

Where, L_w = weir length, m

$$D_c = \text{Column diameter, m}$$

Now,

$$\Theta_c = 2 * \sin^{-1}(L_w / D_c) = 2 * \sin^{-1}(0.77) = 100.7^\circ$$

Now,

$$A_c = (\pi/4) * D_c^2 = 0.785 * D_c^2, \text{ m}^2$$

$$A_d = [(\pi/4) * D_c^2 * (\Theta_c/360^\circ)] - [(L_w/2) * (D_c/2) * \cos(\Theta_c/2)]$$

$$\text{i.e., } A_d = [0.785 * D_c^2 * (100.7^\circ/360^\circ)] - [(1/4) * (L_w / D_c) * D_c^2 * \cos(100.7^\circ)]$$

$$\text{i.e., } A_d = (0.2196 * D_c^2) - (0.1288 * D_c^2)$$

$$\text{i.e., } A_d = 0.0968 * D_c^2, \text{ m}^2$$

Since $A_n = A_c - A_d$

$$0.522 = (0.785 * D_c^2) - (0.0968 * D_c^2)$$

$$\text{i.e., } 0.6882 * D_c^2 = 0.522$$

$$\Rightarrow D_c^2 = 0.522 / 0.6882 = 0.7585$$

$$\Rightarrow D_c = \sqrt{0.7585}$$

$$D_c = 0.87 \text{ m}$$

$$\text{Since } L_w / D_c = 0.77,$$

$$\Rightarrow L_w = 0.77 * D_c = 0.77 * 0.87 = 0.67 \text{ m.}$$

Therefore, $L_w = 0.67 \text{ m.}$

Now,

$$A_c = 0.785 * 0.87^2 = 0.5944 \text{ m}^2$$

$$A_d = 0.0968 * D_c^2 = 0.0968 * 0.87^2 = 0.0724 \text{ m}^2$$

$$A_a = A_c - 2 * A_d$$

$$\text{i.e., } A_a = 0.5944 - 2 * 0.0724 \Rightarrow A_a = 0.4496 \text{ m}^2$$

7. Perforated plate area (A_p):

Now,

$$L_w / D_c = 0.67 / 0.87 = 0.7701$$

$$\Theta_c = 100.73^{\circ}$$

$$\alpha = 180^{\circ} - \Theta_c$$

$$\text{i.e., } \alpha = 180^{\circ} - 100.73^{\circ}$$

$$\Rightarrow \alpha = 79.27^{\circ}$$

Now,

$$A_{cz} = 2 * L_w * (\text{thickness of distribution})$$

Where, A_{cz} = area of calming zone, m^2 (5 to 20% of A_c)

$$A_{cz} = 2 * 0.67 * (30 \times 10^{-3}) = 0.0402 \text{ m}^2 \text{ ----- (which is 6.76\% of } A_c)$$

Also,

$$A_{wz} = 2 * \{ (\pi/4) * D_c^2 * (\Theta_c / 360^{\circ}) - (\pi/4) * (D_c - 30 * 10^{-3})^2 * (\Theta_c / 360^{\circ}) \}$$

Where, A_{wz} = area of waste periphery, m^2 (range 2 to 5% of A_c)

$$\text{i.e., } A_{wz} = 2 * \{ (\pi/4) * 0.87^2 * (100.73^{\circ} / 360^{\circ}) - (\pi/4) * (0.87 - 30 * 10^{-3})^2 * (100.73^{\circ} / 360^{\circ}) \}$$

$$\text{i.e., } A_{wz} = 0.0225 \text{ m}^2 \text{ ----- (which is 3.8\% of } A_c)$$

Now,

$$A_p = A_c - (2 * A_d) - A_{cz} - A_{wz}$$

$$\text{i.e., } A_p = 0.5944 - (2 * 0.0724) - 0.0402 - 0.0225$$

$$\text{Thus, } A_p = 0.387 \text{ m}^2.$$

8. Total Hole Area (A_h):

Since,

$$A_h / A_p = 0.1$$

$$\Rightarrow A_h = 0.1 * A_p$$

$$\text{i.e., } A_h = 0.1 * 0.387$$

$$\Rightarrow A_h = 0.0387 \text{ m}^2$$

Thus, Total Hole Area = 0.0387 m^2

Now we know that,

$$A_h = n_h * (\pi/4) * d_h^2$$

Where, n_h = number of holes.

$$\Rightarrow n_h = (4 * A_h) / (\pi * d_h^2)$$

$$\text{i.e., } n_h = (4 * 0.0387) / (\pi * 0.005^2)$$

$$\Rightarrow n_h \approx 1971$$

Therefore, Number of holes = 1971.

9. Weir Height (h_w):

Let $h_w = 50$ mm.

10. Weeping Check

The static pressure below the tray should be capable enough to hold the liquid above the tray so that no liquid sweeps through the holes.

All the pressure drops calculated in this section are represented as mm head of liquid on the plate. This serves as a common basis for evaluating the pressure drops.

Notations used and their units:

h_d = Pressure drop through the dry plate, mm of liquid on the plate

u_h = Vapor velocity based on the hole area, m/s

h_{ow} = Height of liquid over weir, mm of liquid on the plate

h_{σ} = Pressure drop due to bubble formation, mm of liquid

h_{ds} = Dynamic seal of liquid, mm of liquid

h_1 = Pressure drop due to foaming, mm of liquid

h_f = Pressure drop due to foaming, actual, mm of liquid

D_f = Average flow length of the liquid, m

R_h = Hydraulic radius of liquid flow, m

u_f = Velocity of foam, m/s

(N_{Re}) = Reynolds number of flow

f = Friction factor

h_{hg} = Hydraulic gradient, mm of liquid

h_{da} = Loss under down comer apron, mm of liquid

A_{ds} = Area under the down comer apron, m^2

c = Down comer clearance, m

h_{dc} = Down comer backup, mm of liquid

Calculations:

Head loss through dry hole

h_d = head loss across the dry hole

$$h_d = k_1 + [k_2 * (\rho_g/\rho_l) * U_h^2] \text{ ----- (eq}^n \text{ 18.6, page 18.9, 6}^{\text{th}} \text{ edition Perry)}$$

Where, U_h = gas velocity through hole area

k_1, k_2 are constants

For sieve plates,

$$k_1 = 0 \quad \text{and}$$

$$k_2 = 50.8 / (C_v)^2$$

Where, C_v = discharge coefficient, taken from fig 18.14, page 18.9 6th edition Perry.

Now,

$$(A_h/A_a) = 0.0387/ 0.4496 = 0.086$$

Also, $t_T/d_h = 3/5 = 0.60$

Thus for $(A_h/A_a) = 0.086$ and $t_T/d_h = 0.60$

We have from fig. edition 18.14, page 18.9 6th Perry.

$$C_v = 0.74$$

$$\Rightarrow k_2 = 50.8 / 0.74^2 = 92.77$$

Volumetric flow rate of Vapor at the top of the Enriching Section

$$= q_t = 1.8956/ (3.4376) = 0.5514 \text{ m}^3/\text{s} \text{ ----- (minimum at top)}$$

Volumetric flow rate of Vapor at the bottom of the Enriching Section

$$= q_o = 1.897 / (3.425) = 0.554 \text{ m}^3/\text{s}. \text{ ---- (maximum at bottom)}$$

Velocity through the hole area (U_h):

Now,

$$\text{Velocity through the hole area at the top} = U_{h, \text{top}} = q_t/A_h$$

$$= 0.5514/0.0387 = 14.25 \text{ m/s}$$

Also, Velocity through the hole area at the bottom = $U_{h, \text{bottom}} = q_o/A_h$

$$= 0.554/0.0387 = 14.31 \text{ m/s}$$

Now,

$$h_{d, \text{top}} = k_2 [\rho_g/\rho_l] (U_{h, \text{top}})^2$$

$$= 92.77 * (3.4376/784.69) * 14.25^2$$

$$\Rightarrow h_{d, \text{top}} = 82.526 \text{ mm clear liquid. ----- (minimum at top)}$$

Also,

$$\begin{aligned} h_{d, \text{bottom}} &= k_2 [\rho_g/\rho_l] (U_{h, \text{bottom}})^2 \\ &= 92.77*(3.425/784.50)\times 14.31^2 \end{aligned}$$

$$\Rightarrow h_{d, \text{bottom}} = \underline{82.94} \text{ mm clear liquid ----- (maximum at bottom)}$$

Head Loss Due to Bubble Formation

$$h_\sigma = 409 [\sigma / (\rho_L * d_h)]$$

where σ = surface tension, mN/m (dyne/cm) = 19.325 dyne/cm.

d_h = Hole diameter, mm

ρ_l = density of liquid in the section, kg/m³

$$= 784.69 \text{ kg/m}^3$$

$$h_\sigma = 409 [19.325 / (784.69 * 5)]$$

$$h_\sigma = 2.014 \text{ mm clear liquid}$$

Height of Liquid Crest over Weir:

$$h_{ow} = 664 * F_w [(q/L_w)^{2/3}]$$

q = liquid flow rate at top, m³/s

$$= 0.1263 * 60 / (784.69)$$

$$= 0.009 \text{ m}^3/\text{min.}$$

Thus, $q' = 2.377 \text{ gal/min.}$

$$L_w = \text{weir length} = 0.67 \text{ m} = 2.198 \text{ ft}$$

Now,

$$q'/L_w^{2.5} = 2.377 / (2.198)^{2.5} = 0.3318$$

Now for $q'/L_w^{2.5} = 0.3318$ and $L_w/D_c = 0.7701$

We have from fig.18.16, page 18.11, 6th edition Perry

$$F_w = \text{correction factor} = 1.03$$

$$\text{Thus, } h_{ow} = 1.03 * 664 * [0.00015 / 0.67]^{2/3}$$

$$\Rightarrow h_{ow} = 2.52 \text{ mm clear liquid.}$$

Now,

$$(h_d + h_\sigma) = 82.526 + 2.014 = 84.54 \text{ mm} \text{ ----- Design value}$$

$$(h_w + h_{ow}) = 50 + 2.52 = 52.52 \text{ mm}$$

For, $A_h/A_a = 0.086$ and $(h_w + h_{ow}) = 52.52 \text{ mm}$

The minimum value of $(h_d + h_\sigma)$ required is calculated from a graph given in Perry, plotted against A_h/A_a .

i.e., we have from fig. 18.11, page 18.7, 6th edition Perry

$$(h_d + h_\sigma)_{\min} = \underline{13.0} \text{ mm} \text{ ----- Theoretical value.}$$

The minimum value as found is 13.0 mm.

Since the design value is greater than the minimum value, **there is no problem of weeping.**

Down comer Flooding:

$$h_{ds} = h_w + h_{ow} + (h_{hg}/2) \text{ ----- (eq}^n \text{ 18.10, page 18.10, 6}^{\text{th}} \text{ edition Perry)}$$

Where,

h_w = weir height, mm

h_{ds} = static slot seal (weir height minus height of top of slot above plate floor, height equivalent clear liquid, mm)

h_{ow} = height of crest over weir, equivalent clear liquid, mm

h_{hg} = hydraulic gradient across the plate, height of equivalent clear liquid, mm.

Hydraulic gradient, h_{hg}

Let $h_{hg} = 0.5 \text{ mm}$.

$$\begin{aligned} h_{ds} &= h_w + h_{ow} + h_{hg}/2 \\ &= 50 + 2.52 + 0.5/2 = 52.77 \text{ mm.} \end{aligned}$$

Now, $F_{ga} = U_a * \rho_g^{0.5}$

Where F_{ga} = gas-phase kinetic energy factor,

U_a = superficial gas velocity, m/s (ft/s),

ρ_g = gas density, kg/m³ (lb/ft³)

Here U_a is calculated at the bottom of the section.

Thus, $U_a = (G_b/\rho_g) / A_a = 1.8974 / (3.425 * 0.4496) = 1.232 \text{ m/s}$

Thus, $U_a = 4.042 \text{ ft/s}$

$$\rho_g = 3.4250 \text{ kg/m}^3 = 0.209 \text{ lb/ft}^3$$

Therefore, $F_{ga} = 4.042 * (0.209)^{0.5}$

$$F_{ga} = 1.848$$

Now for $F_{ga} = 1.848$, we have from fig. 18.15, page 18.10 6th edition Perry

$$\text{Aeration factor} = \beta = 0.6$$

$$\text{Relative Froth Density} = \phi_t = 0.2$$

Now $h_l' = \beta * h_{ds}$ ---- (eqⁿ 18.8, page 18.10, 6th edition Perry)

Where, h_l' = pressure drop through the aerated mass over and around the disperser, mm liquid,

$$\Rightarrow h_l' = 0.6 * 52.77 = 31.662 \text{ mm.}$$

Now,

$$h_f = h_l' / \phi_t \text{ ----- (eqⁿ 18.9, page 18.10, 6th edition Perry)}$$

$$\Rightarrow h_f = 31.662 / 0.2 = 158.31 \text{ mm.}$$

Average width of liquid flow path, $D_f = (D_c + L_w) / 2$

$$= (0.87 + 0.67) / 2 = 0.77 \text{ m.}$$

Hydraulic radius of aerated mass $R_h = h_f * D_f / (2 * h_f + 1000 * D_f)$ (from eq. 18.23, page 18.12 6th edition Perry)

$$R_h = 158.31 * 0.77 / (2 * 158.31 + 1000 * 0.77)$$

$$= 0.112 \text{ m.}$$

Velocity of aerated mass, $U_f = 1000 * q / (h_l' * D_f)$

Volumetric flow rate, $q = 1.6061 * 10^{-4} \text{ m}^3/\text{s.}$

$$U_f = 1000 * 1.6061 * 10^{-4} / (31.662 * 0.77)$$

$$= 0.0066 \text{ m/s.}$$

Reynolds modulus $N_{Re} = R_h * U_f * \rho_l / \mu_{liq}$

$$= 0.112 * 0.0066 * 784.5 / (1.03 * 10^{-3})$$

$$= 563.012$$

$$h_{hg} = 1000 * f * U_f^2 * L_f / (g * R_h)$$

$$f = 0.6 \text{ for } h_w = 1.97'' \text{ and } N_{Re} = 563.012$$

$$L_f = 2 * D_c / 2 \cos (\Theta_c / 2) = 0.5549 \text{ m}$$

$$h_{hg} = 1000 * 0.6 * 0.0066^2 * 0.5549 / (9.81 * 0.112)$$

$$= 0.0132 \text{ mm.}$$

Head loss over down comer apron:

$$h_{da} = 165.2 \{q/ A_{da}\}^2 \text{ ----- (eq}^n \text{ 18.19, page 18.10, 6}^{\text{th}} \text{ edition Perry)}$$

Where, h_{da} = head loss under the down comer apron, as millimeters of liquid,

q = liquid flow rate calculated at the bottom of section, m^3/s

And A_{da} = minimum area of flow under the down comer apron, m^2

Now,

$$q = 1.6061 * 10^{-4} \text{ m}^3/\text{s}$$

Take clearance, $C = 1'' = 25.4 \text{ mm}$

$$h_{ap} = h_{ds} - C = 52.77 - 25.4 = 27.37 \text{ mm}$$

$$A_{da} = L_w * h_{ap} = 0.67 * 27.37 * 10^{-3} = 0.0183 \text{ m}^2$$

$$h_{da} = 165.2 [(1.6061 * 10^{-4}) / (0.0183)]^2$$

$$h_{da} = 0.0127 \text{ mm}$$

Now,

$$h_t = h_d + h_l'$$

Here h_d and h_l' are calculated at bottom of the enriching section.

Now we have,

$$h_{d, \text{bottom}} = 82.94 \text{ mm}$$

$$h_{l, \text{bottom}} = 31.662 \text{ mm}$$

$$h_t = h_d + h_l'$$

$$= 82.94 + 31.662$$

$$h_t = 114.602 \text{ mm}$$

Down comer Backup:

$$h_{dc} = h_t + h_w + h_{ow} + h_{da} + h_{hg} \text{ ----- (eq}^n \text{ 18.3, page 18.7, 6}^{\text{th}} \text{ edition Perry)}$$

h_t = total pressure drop across the plate (mm liquid)

$$= h_d + h_l'$$

h_{dc} = height in down comer, mm liquid,

h_w = height of weir at the plate outlet, mm liquid,

h_{ow} = height of crest over the weir, mm liquid,

h_{da} = head loss due to liquid flow under the down comer apron, mm liquid,

h_{hg} = liquid gradient across the plate, mm liquid.

$$h_{dc} = 114.602 + 50 + 2.52 + 0.0132 + 0.0127$$

$$h_{dc} = 167.148 \text{ mm.}$$

Let ϕ_{dc} = average relative froth density (ratio of froth density to liquid density)
= 0.5

$$h'_{dc} = h_{dc} / \phi_{dc} = 167.148 / 0.5$$

$$h'_{dc} = 334.29 \text{ mm.}$$

which is less than the tray spacing, $t_s = 457 \text{ mm}$.

Hence no flooding in the enriching section and hence the design calculations are acceptable.

b). Design of Stripping Section:

Tray Hydraulics

The design of a sieve plate tower is described below. The equations and correlations are borrowed from the 6th and 7th editions of Perry's Chemical Engineers' Handbook.

1 Tray Spacing, (t_s) :

$$\text{Let } t_s = 18'' = 457 \text{ mm.}$$

2 Hole Diameter, (d_h):

$$\text{Let } d_h = 5 \text{ mm.}$$

3 Hole Pitch (l_p):

$$\text{Let } l_p = 3 * d_h$$

$$\text{i.e., } l_p = 3 * 5 = 15 \text{ mm.}$$

4 Tray thickness (t_T):

$$\text{Let } t_T = 0.6 * d_h$$

$$\text{i.e., } t_T = 0.6 * 5 = 3 \text{ mm.}$$

5 Ratio of hole area to perforated area (A_h/A_p):

Refer fig 3

Now, for a triangular pitch, we know that,

$$\text{Ratio of hole area to perforated area } (A_h/A_p) = \frac{1}{2} (p/4 * d_h^2) / [(\sqrt{3}/4) * l_p^2]$$

$$\text{i.e., } (A_h/A_p) = 0.90 * (d_h/l_p)^2$$

$$\text{i.e., } (A_h/A_p) = 0.90 * (5/15)^2$$

$$\text{i.e., } (A_h/A_p) = 0.1$$

Thus,

$$(A_h/A_p) = 0.1$$

6 Plate Diameter (D_c):

The plate diameter is calculated based on the flooding considerations

$$L/G \{ \rho_g / \rho_l \}^{0.5} = 0.0705 \quad \text{----- (maximum value)}$$

Now for,

$$L/G \{ \rho_g / \rho_l \}^{0.5} = 0.0705 \text{ and for a tray spacing of 457 mm.}$$

We have,

From the flooding curve, ----- (fig.18.10, page 18.7, 6th edition Perry.)

$$\text{Flooding parameter, } C_{sb, flood} = 0.27 \text{ ft/s.}$$

Now,

$$U_{nf} = C_{sb, flood} * (\sigma / 20)^{0.2} [(\rho_l - \rho_g) / \rho_g]^{0.5}$$

---- {eqⁿ. 18.2, page 18.6, 6th edition Perry. }

where,

U_{nf} = gas velocity through the net area at flood, m/s (ft/s)

$C_{sb, flood}$ = capacity parameter, m/s (ft/s, as in fig.18.10)

σ = liquid surface tension, mN/m (dyne/cm.)

ρ_l = liquid density, kg/m³ (lb/ft³)

ρ_g = gas density, kg/m³ (lb/ft³)

Now, we have,

$$\sigma = 18.330 \text{ mN/m} = 18.330 \text{ dyne/cm.}$$

$$\rho_l = 747.87 \text{ kg/m}^3.$$

$$\rho_g = 3.361 \text{ kg/m}^3.$$

Therefore,

$$U_{nf} = 0.27 * (18.33/20)^{0.2} \times [(747.87-3.361) / 3.361]^{0.5}$$

$$\text{i.e., } U_{nf} = 3.949 \text{ ft/s}$$

Let,

$$\text{Actual velocity, } U_n = 0.8 * U_{nf}$$

$$\text{i.e., } U_n = 0.8 * 3.949$$

$$\text{i.e., } U_n = 3.159 \text{ ft/s}$$

$$U_n = 0.9628 \text{ m/s}$$

Now,

Volumetric flow rate of Vapor at the bottom of the Stripping Section

$$= q_o = 1.9657 / (3.361) = 0.5848 \text{ m}^3/\text{s}.$$

Now,

Net area available for gas flow (A_n)

Net area = (Column cross sectional area) - (Down comer area.)

$$A_n = A_c - A_d$$

Thus,

$$\text{Net Active area, } A_n = q_o / U_n = 0.5848 / 0.9628 = 0.6074 \text{ m}^2.$$

$$\text{Let } L_w / D_c = 0.77$$

Where, L_w = weir length, m

D_c = Column diameter, m

Now,

$$\theta_c = 2 * \sin^{-1}(L_w / D_c) = 2 * \sin^{-1}(0.77) = 100.7^\circ$$

Now,

$$A_c = (\pi/4) * D_c^2 = 0.785 * D_c^2, \text{ m}^2$$

$$A_d = [(\pi/4) * D_c^2 * (\theta_c/360^\circ)] - [(L_w/2) * (D_c/2) * \cos(\theta_c/2)]$$

$$\text{i.e., } A_d = [0.7854 * D_c^2 * (100.7^\circ/360^\circ)] - [(1/4) * (L_w / D_c) * D_c^2 * \cos(100.7^\circ/2)]$$

$$\text{i.e., } A_d = (0.2196 * D_c^2) - (0.1288 * D_c^2)$$

$$\text{i.e., } A_d = 0.0968 * D_c^2, \text{ m}^2$$

Since $A_n = A_c - A_d$

$$0.6882 = (0.785 * D_c^2) - (0.0968 * D_c^2)$$

$$\text{i.e., } 0.6882 * D_c^2 = 0.6074$$

$$\Rightarrow D_c^2 = 0.6074 / 0.6882 = 0.8826$$

$$\Rightarrow D_c = \sqrt{0.8826}$$

$$D_c = 0.94 \text{ m}$$

Therefore, $D_c = 0.94$ m

Since $L_w / D_c = 0.77$

$$\Rightarrow L_w = 0.77 * D_c = 0.77 * 0.94 = 0.724 \text{ m.}$$

Therefore, $L_w = 0.724$ m.

Now,

$$A_c = 0.785 * 0.94^2 = 0.694 \text{ m}^2$$

$$A_d = 0.09688 * D_c^2 = 0.0968 * 0.94^2 = 0.0866 \text{ m}^2$$

$$A_n = A_c - A_d$$

$$\text{i.e., } A_n = 0.694 - 0.0866$$

$$\Rightarrow A_n = 0.6074 \text{ m}^2$$

7 Perforated plate area (A_p):

$$A_a = A_c - (2 * A_d)$$

$$\text{i.e., } A_a = 0.694 - (2 * 0.0866)$$

$$\Rightarrow A_a = 0.5208 \text{ m}^2$$

Now,

$$L_w / D_c = 0.724 / 0.94 = 0.7702$$

$$\Theta_c = 100.746^\circ$$

$$\alpha = 180^\circ - \Theta_c$$

$$\text{i.e., } \alpha = 180^\circ - 100.746^\circ$$

$$\Rightarrow \alpha = 79.254^\circ$$

Now,

$$A_{cz} = 2 * L_w * (\text{thickness of distribution})$$

Where, A_{cz} = area of calming zone, m^2

$$A_{cz} = 2 * 0.724 * (30 * 10^{-3}) = 0.04344 \text{ m}^2 \text{ ----- (which is 6.26\% of } A_c)$$

Also,

$$A_{wz} = 2 * \{ (\pi/4) * D_c^2 * (\Theta_c / 360^\circ) - (\pi/4) * (D_c - 0.03)^2 * (\Theta_c / 360^\circ) \}$$

Where, A_{wz} = area of waste periphery, m^2

$$\text{i.e., } A_{wz} = 2 * \{ (\pi/4) * 0.94^2 * (100.746^\circ / 360^\circ) \}$$

$$- (\pi/4) * (0.94 - 0.03)^2 * (100.746^\circ / 360^\circ) \}$$

i.e., $A_{wz} = 0.0244 \text{ m}^2$ ----- (which is 3.515% of A_c)

Now,

$$A_p = A_c - (2 * A_d) - A_{cz} - A_{wz}$$

$$\text{i.e., } A_p = 0.694 - (2 * 0.0866) - 0.04344 - 0.0244$$

$$\text{Thus, } A_p = 0.453 \text{ m}^2$$

8 Total Hole Area (A_h):

Since,

$$A_h / A_p = 0.1$$

$$\Rightarrow A_h = 0.1 * A_p$$

$$\text{i.e., } A_h = 0.1 * 0.453$$

$$\Rightarrow A_h = 0.0453 \text{ m}^2$$

$$\text{Thus, Total Hole Area} = 0.04147 \text{ m}^2$$

Now we know that,

$$A_h = n_h * (\pi/4) * d_h^2$$

Where n_h = number of holes.

$$\Rightarrow n_h = (4 * A_h) / (\pi * d_h^2)$$

$$\text{i.e., } n_h = (4 * 0.0453) / (\pi * 0.005^2)$$

$$\Rightarrow n_h = 2307.21 \approx 2308$$

Therefore, Number of holes = 2308.

9 Weir Height (h_w):

Let, $h_w = 50 \text{ mm}$.

10 Weeping Check

All the pressure drops calculated in this section are represented as mm head of liquid on the plate. This serves as a common basis for evaluating the pressure drops.

Notations used and their units:

h_d = Pressure drop through the dry plate, mm of liquid on the plate

u_h = Vapor velocity based on the hole area, m/s

h_{ow} = Height of liquid over weir, mm of liquid on the plate
 h_{σ} = Pressure drop due to bubble formation, mm of liquid
 h_{ds} = Dynamic seal of liquid, mm of liquid
 h_l = Pressure drop due to foaming, mm of liquid
 h_f = Pressure drop due to foaming, actual, mm of liquid
 D_f = Average flow length of the liquid, m
 R_h = Hydraulic radius of liquid flow, m
 U_f = Velocity of foam, m/s
 (N_{Re}) = Reynolds number of flow
 f = Friction factor
 h_{hg} = Hydraulic gradient, mm of liquid
 h_{da} = Loss under down comer apron, mm of liquid
 A_{da} = Area under the down comer apron, m²
 C = Down comer clearance, m
 h_{dc} = Down comer backup, mm of liquid

Calculations:

Head loss through dry hole

h_d = head loss across the dry hole

$$h_d = k_1 + [k_2 * (\rho_g/\rho_l) * U_h^2] \text{ ----- (eq}^n \text{ 18.6, page 18.9, 6}^{\text{th}} \text{ edition Perry)}$$

where U_h = gas velocity through hole area

k_1, k_2 are constants

For sieve plates

$$k_1 = 0 \quad \text{and}$$

$$k_2 = 50.8 / (C_v)^2$$

where C_v = discharge coefficient, taken from fig. edition 18.14, page 18.9 6th Perry).

Now,

$$(A_h/A_a) = 0.0453 / 0.5208 = 0.087$$

$$\text{also } t_T/d_h = 3/5 = 0.60$$

Thus for $(A_h/A_a) = 0.087$ and $t_T/d_h = 0.60$

We have from fig. edition 18.14, page 18.9 6th Perry.

$$C_v = 0.73$$

$$\Rightarrow k_2 = 50.8 / 0.73^2 = 95.327$$

Volumetric flow rate of Vapor at the top of the Stripping Section

$$= q_t = 1.8974 / (3.425) = 0.554 \text{ m}^3/\text{s} \text{ ----- (minimum at top)}$$

Volumetric flow rate of Vapor at the bottom of the Stripping Section

$$= q_o = 1.9657 / (3.361) = 0.5848 \text{ m}^3/\text{s}. \text{ ----- (maximum at bottom).}$$

Velocity through the hole area (U_h):

Now,

$$\begin{aligned} \text{Velocity through the hole area at the top} &= U_{h, \text{ top}} = q_t / A_h \\ &= 0.554 / 0.0453 = 12.23 \text{ m/s} \end{aligned}$$

also, Velocity through the hole area at the bottom = $U_{h, \text{ bottom}} = q_o / A_h$

$$= 0.5848 / 0.0453 = 12.91 \text{ m/s}$$

Now,

$$\begin{aligned} h_{d, \text{ top}} &= k_2 [\rho_g / \rho_l] (U_{h, \text{ top}})^2 \\ &= 95.327 * (3.425 / 784.50) * 12.23^2 \end{aligned}$$

$$\Rightarrow h_{d, \text{ top}} = 62.25 \text{ mm clear liquid. ----- (minimum at top)}$$

also

$$\begin{aligned} h_{d, \text{ bottom}} &= k_2 [\rho_g / \rho_l] (U_{h, \text{ bottom}})^2 \\ &= 95.327 * (3.361 / 747.87) * 12.91^2 \end{aligned}$$

$$\Rightarrow h_{d, \text{ bottom}} = 71.4 \text{ mm clear liquid ----- (maximum at bottom)}$$

Head Loss Due to Bubble Formation

$$h_\sigma = 409 [\sigma / (\rho_L * d_h)]$$

Where σ = surface tension, mN/m (dyne/cm)

d_h = Hole diameter, mm

ρ_l = average density of liquid in the section, kg/m³

$$\rho_l = 784.5 \text{ kg/m}^3$$

$$h_{\sigma} = 409 [18.33 / (784.5 * 5)]$$

$$h_{\sigma} = 1.911 \text{ mm clear liquid.}$$

Height of Liquid Crest over Weir

$$h_{ow} = 664 * F_w [(q/L_w)^{2/3}]$$

$$q = \text{liquid flow rate at top, m}^3/\text{s}$$

$$= 0.0035 \text{ m}^3/\text{s.}$$

$$q' = 1.998 * 60 / 7193.9 = 0.0166 \text{ m}^3/\text{min} = 4.384 \text{ gal/min.}$$

Thus, $q' = 4.384 \text{ gal/min.}$

$$L_w = \text{weir length} = 0.724 \text{ m} = 2.3753 \text{ ft}$$

Now,

$$q'/L_w^{2.5} = 4.384 / (2.375)^{2.5} = 0.504$$

Now for $q'/L_w^{2.5} = 0.504$ and $L_w/D_c = 0.7702$

We have from fig. 18.16, page 18.11, 6th edition Perry

$$F_w = \text{correction factor} = 1.02$$

$$\text{Thus, } h_{ow} = 1.02 \times 664 \times [(0.00035)/0.724]^{2/3}$$

$$\Rightarrow h_{ow} = 4.17 \text{ mm clear liquid.}$$

Now,

$$(h_d + h_{\sigma}) = 62.25 + 1.911 = 64.161 \text{ mm} \text{ ----- Design value}$$

$$(h_w + h_{ow}) = 50 + 4.17 = 54.17 \text{ mm}$$

Also, $A_h/A_a = 0.087$ and $(h_w + h_{ow}) = 50 + 4.17 = 54.17 \text{ mm}$

The minimum value of $(h_d + h_{\sigma})$ required is calculated from a graph given in Perry, plotted against A_h/A_a .

i.e., we have from fig. 18.11, page 18.7, 6th edition Perry

$$(h_d + h_{\sigma})_{\min} = 12.0 \text{ mm} \text{ ----- Theoretical value.}$$

The minimum value as found is 12.0 mm.

Since the design value is greater than the minimum value, **there is no problem of weeping.**

Down comer Flooding:

$$h_{ds} = h_w + h_{ow} + (h_{hg}/2) \text{ ----- (eq}^n \text{ 18.10, page 18.10, 6}^{\text{th}} \text{ edition Perry)}$$

Where,

h_w = weir height, mm

h_{ds} = static slot seal (weir height minus height of top of slot above plate floor, height equivalent clear liquid, mm)

h_{ow} = height of crest over weir, equivalent clear liquid, mm

h_{hg} = hydraulic gradient across the plate, height of equivalent clear liquid, mm.

Hydraulic gradient, h_{hg}

Let $h_{hg} = 0.5$ mm.

$$\begin{aligned} h_{ds} &= h_w + h_{ow} + h_{hg}/2 \\ &= 50 + 4.17 + 0.5/2 = 54.42 \text{ mm.} \end{aligned}$$

Now, $F_{ga} = U_a * \rho_g^{0.5}$

Where F_{ga} = gas-phase kinetic energy factor,

U_a = superficial gas velocity, m/s (ft/s),

ρ_g = gas density, kg/m³ (lb/ft³)

Here U_a is calculated at the bottom of the section.

Thus, $U_a = (G_b/\rho_g) / A_a = 1.9657 / (0.5208*3.361) = 1.123$ m/s

Thus, $U_a = \underline{3.684}$ ft/s

$\rho_g = 3.361$ kg/m³ = 0.205 lb/ft³

Therefore, $F_{ga} = 3.684 * (0.205)^{0.5}$

$$F_{ga} = 1.668$$

Now for $F_{ga} = 1.668$, we have from fig. 18.15, page 18.10 6th edition Perry)

Aeration factor = $\beta = 0.61$

Relative Froth Density = $\phi_t = 0.21$

Now $h_1' = \beta * h_{ds}$ ---- (eqⁿ. 18.8, page 18.10, 6th edition Perry)

Where, h_1' = pressure drop through the aerated mass over and around the disperser, mm liquid,

$$\Rightarrow h_1' = 0.61 * 54.42 = \underline{33.1962} \text{ mm.}$$

Now,

$h_f = h_1' / \phi_t$ ----- (eqⁿ. 18.9, page 18.10, 6th edition Perry)

$$\Rightarrow h_f = 33.1962 / 0.21 = 158.07 \text{ mm.}$$

Average width of liquid flow path, $D_f = (D_c + L_w)/2$
 $= (0.94 + 0.724)/2 = 0.832 \text{ m.}$

Hydraulic radius of aerated mass $R_h = h_f \cdot D_f / (2 \cdot h_f + 1000 \cdot D_f)$ (from eq. 18.23, page 18.12 6th edition Perry)

$$R_h = 158.07 \cdot 0.832 / (2 \cdot 158.07 + 1000 \cdot 0.832)$$

$$= 0.1145 \text{ m.}$$

Velocity of aerated mass, $U_f = 1000 \cdot q / (h_l \cdot D_f)$

Volumetric flow rate, $q = 2.068 / 747.87 = 0.00276 \text{ m}^3/\text{s.}$

$$U_f = 1000 \cdot 0.00276 / (33.1962 \cdot 0.832)$$

$$= 0.0999 \text{ m/s.}$$

Reynolds modulus $N_{Re} = R_h \cdot U_f \cdot \rho_l / \mu_{liq}$

$$= 0.1145 \cdot 0.0999 \cdot 747.87 / (0.924 \cdot 10^{-3})$$

$$= 9257.17$$

$$h_{hg} = 1000 \cdot f \cdot U_f^2 \cdot L_f / (g \cdot R_h)$$

$$f = 0.18 \text{ for } h_w = 1.97'' \text{ and } N_{Re} = 9257.17$$

$$L_f = 2 \cdot D_c / 2 \cos (\Theta_c / 2) = 0.5995 \text{ m.}$$

$$h_{hg} = 1000 \cdot 0.18 \cdot 0.0999^2 \cdot 0.5995 / (9.81 \cdot 0.1145)$$

$$= 0.958 \text{ mm.}$$

Head loss over down comer apron:

$$h_{da} = 165.2 \{q / A_{da}\}^2 \text{ ----- (eq}^n \text{ 18.19, page 18.10, 6}^{\text{th}} \text{ edition Perry)}$$

Where, h_{da} = head loss under the down comer apron, as millimeters of liquid,

q = liquid flow rate calculated at the bottom of section, m^3/s

And A_{da} = minimum area of flow under the down comer apron, m^2

Now,

$$q = 0.00276 \text{ m}^3/\text{s}$$

Take clearance, $C = 1'' = 25.4 \text{ mm}$

$$h_{ap} = h_{ds} - C = 54.42 - 25.4 = 29.02 \text{ mm}$$

$$A_{da} = L_w \times h_{ap} = 0.724 \cdot 29.03 \cdot 10^{-3} = 0.021 \text{ m}^2$$

$$h_{da} = 165.2 [(0.00276) / (0.021)]^2$$

$$h_{da} = 2.85 \text{ mm}$$

Now

$$h_t = h_d + h_i'$$

Here h_d and h_i' are calculated at bottom of the Stripping section.

Now we have,

$$h_{d, \text{bottom}} = 71.4 \text{ mm}$$

$$h_{i, \text{bottom}} = 33.1962 \text{ mm}$$

$$h_t = h_d + h_i'$$

$$= 71.4 + 33.1962$$

$$h_t = 104.6 \text{ mm}$$

Down comer Backup:

$$h_{dc} = h_t + h_w + h_{ow} + h_{da} + h_{hg} \text{ ---- (eq}^n \text{ 18.3, page 18.7, 6}^{\text{th}} \text{ edition Perry)}$$

h_t = total pressure drop across the plate (mm liquid)

$$= h_d + h_i'$$

h_{dc} = height in down comer, mm liquid,

h_w = height of weir at the plate outlet, mm liquid,

h_{ow} = height of crest over the weir, mm liquid,

h_{da} = head loss due to liquid flow under the down comer apron, mm liquid,

h_{hg} = liquid gradient across the plate, mm liquid.

$$h_{dc} = 104.6 + 50 + 4.17 + 0.958 + 2.85$$

$$h_{dc} = 162.58 \text{ mm.}$$

Let ϕ_{dc} = average relative froth density (ratio of froth density to liquid density) =

0.5

$$h'_{dc} = h_{dc} / \phi_{dc} = 162.58 / 0.5$$

$$h'_{dc} = 325.16 \text{ mm.}$$

Which is less than the tray spacing, $t_s = 457 \text{ mm}$.

Hence no flooding in the Stripping section and hence the design calculations are acceptable.

Formulas used in calculation of properties:

1 VISCOSITY:

(i). Average Liquid Viscosity:

$$(\mu_{\text{liq}})^{1/3} = [x_1 \times (\mu_1)^{1/3}] + [x_2 \times (\mu_2)^{1/3}]$$

2 DIFFUSIVITIES:

(i). Liquid Phase Diffusivity:

For the case of Organic solutes diffusing in Organic solvents

$$D_{AB} = (1.173 \times 10^{-13} \times (\Theta \cdot M)^{0.5} \cdot T) / [\eta_B \times (V_A)^{0.6}] \text{---(Richardson - coulson vol.6)}$$

Where,

Θ = constant

M = molecular weight.

T = absolute temperature, $^{\circ}\text{K}$,

η_B = viscosity of solvent B, cP,

V_A = molar volume of solute A at its normal boiling temperature, $\text{cm}^3/\text{g-mol}$.

D_{AB} = mutual diffusivity coefficient of solute A at very low concentration in solvent B, cm^2/s

(ii). Gas Phase Diffusivity:

$$D_{AB} = 1.013 \times 10^{-7} \times T^{1.75} \times [(M_A + M_B) / (M_A \times M_B)]^{1/2} / \{P \times [(\sum V_A)^{1/3} + (\sum V_B)^{1/3}]^2\}$$

----- (Richardson - coulson vol.6).

Where P = Pressure in atmospheres,

T = Temperature in $^{\circ}\text{K}$

D_{AB} = Diffusivity, cm^2/s

$\sum V_A$ and $\sum V_B$ = summation of atomic diffusion volumes for components A and B respectively.

M_A and M_B = Molecular weights of components A and B respectively.

3. SURFACE TENSION:

$$\sigma = [P_{\text{ch}} \times (\rho_l - \rho_g) / M]^4 \times 10^{-12} \text{----- (eq}^n \text{ 8.23, page 293, Coulson and Richardson vol.6)}$$

Where,

σ = surface tension, dyne/cm

P_{ch} = Sugden's Parachor,

ρ_l = liquid density, kg/m^3

ρ_g = density of saturated vapor, kg/m^3

M = Molecular weight

σ , ρ_l , and ρ_g are evaluated at system temperature.

$\sigma_{mix} = \sum (x_i \times \sigma_i)$ where $i=1,2,3,\dots,n$.

4. LIQUID DENSITY:

$$\rho = P_c / (R * T_c * Z_c^{[1+(1-T_r)^{2/7}]}) \quad (\text{Coulson and Richardson vol.6})$$

Where,

$$P_c = \text{critical pressure} = M / (0.34 + (\sum \Delta P)^2)$$

M = Molecular weight.

$$T_c = \text{Critical temperature} = T_b / (0.567 + \sum \Delta T - (\sum \Delta T)^2)$$

T_b = Normal boiling temperature $^{\circ}\text{K}$.

$$Z_c = P_c * V_c / (R * T_c)$$

V_c = critical volume

R = universal gas constant.

5. GAS DENSITY:

$$\rho = P * M / (R * T)$$

P = pressure

M = Molecular weight.

R = universal gas constant.

T = temperature.

Enriching section:

Column efficiency (AIChE method)

1. Point Efficiency, (E_{og}):

$$E_{og} = 1 - e^{-N_{og}} = 1 - \exp(-N_{og}) \text{ ----- (eq}^n \text{ 18.33, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where N_{og} = Overall transfer units

$$N_{og} = 1 / [(1/N_g) + (\lambda/N_l)] \text{ ---- (eq}^n \text{ 18.34, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where N_l = Liquid phase transfer units,

N_g = Gas phase transfer units,

$\lambda = (m \cdot G_m) / L_m$ = Stripping factor,

m = slope of Equilibrium Curve,

G_m = Gas flow rate, mol/s

L_m = Liquid flow rate, mol/s

$$N_g = (0.776 + (0.0045 \cdot h_w) - (0.238 \cdot U_a \cdot \rho_g^{0.5}) + (105 \cdot W)) / (N_{Sc, g})^{0.5} \\ \text{----- (eq}^n \text{ 18., page 18., 6}^{\text{th}} \text{ edition Perry)--- *}$$

Where,

h_w = weir height = 50.00 mm

U_a = Gas velocity through active area, m/s

$$= 1.232 \text{ m/s.}$$

$U_a = 1.232 \text{ m/s}$

$D_f = (L_w + D_c) / 2 = (0.87 + 0.67) / 2 = 0.77 \text{ m}$

$q = 161.30 \cdot 10^{-6} \text{ m}^3/\text{s}$

W = Liquid flow rate, $\text{m}^3/(\text{s} \cdot \text{m})$ of width of flow path on the plate,

$$= q / D_f = 161.3 \cdot 10^{-6} / 0.77 = 209.48 \cdot 10^{-6} \text{ m}^3/(\text{s} \cdot \text{m})$$

$N_{Sc, g}$ = Schmidt number = $\mu_g / (\rho_g \cdot D_g) = 0.6256$

D_g = Diffusivity = $4.433 \cdot 10^{-6} \text{ m}^2/\text{s}$.

Now,

Number of gas phase transfer units,

$$N_g = (0.776 + (0.0045 \cdot 50) - (0.238 \cdot 1.232 \cdot 3.425^{0.5}) + (105 \cdot 209.48 \cdot 10^{-6})) / (0.6256)^{0.5}$$

$$10 \quad N_g = 0.6073$$

Also,

Number of liquid phase transfer units,

$$N_l = k_l \cdot a \cdot \theta_l \text{ ---- (eq}^n \text{ 18.36a, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where k_l = Liquid phase transfer coefficient kmol/ (sm² kmol/m³) or m/s

a = effective interfacial area for mass transfer m²/m³ froth or spray on the plate,

θ_l = residence time of liquid in the froth or spray, s

$$\theta_l = (h_l \cdot A_a) / (1000 \cdot q) \text{ ---- (eq}^n \text{ 18.38, page 18.16, 6}^{\text{th}} \text{ edition Perry)}$$

Now, q = liquid flow rate, m³/s

$$q = 161.30 \cdot 10^{-6} \text{ m}^3/\text{s}$$

$$h_l = h_l' = 31.662 \text{ mm}$$

$$A_a = 0.4496 \text{ m}^2$$

$$\theta_l = 31.662 \cdot 0.4496 / (1000 \cdot 161.3 \cdot 10^{-6}) = 88.25 \text{ s}$$

$$k_l \cdot a = (3.875 \cdot 10^8 \cdot D_L)^{0.5} \cdot ((0.40 \cdot U_a \cdot \rho_g^{0.5}) + 0.17)$$

--- (eqⁿ 18.40a, page 18.16, 6th edition Perry)

D_L = liquid phase diffusion coefficient, m²/s

$$k_l \cdot a = (3.875 \cdot 10^8 \cdot 2.002 \cdot 10^{-9})^{0.5} \cdot ((0.40 \cdot 1.232 \cdot 3.425^{0.5}) + 0.17)$$

$$k_l \cdot a = 0.933 \text{ m/s}$$

$$N_l = k_l \cdot a \cdot q_l$$

i.e., $N_l = 0.933 \cdot 88.25$

$$\lambda_m = m_m \cdot G_m / L_m$$

$$\lambda_b = 0.5990$$

$$\lambda_t = 0.3$$

$$\Rightarrow \lambda = 0.4495$$

$$N_{og} = 1 / [(1/N_g) + (\lambda/N_l)]$$

$$= 1 / [(1/1.093) + (0.4495/82.33)]$$

$$N_{og} = 1.0865$$

$$E_{og} = 1 - e^{-N_{og}} = 1 - \exp(-N_{og})$$

$$= 1 - e^{-1.0865} = 1 - \exp(-1.0865)$$

$$E_{og} = 0.6626$$

Point Efficiency = $E_{og} = 0.6626$

2 Murphree Plate Efficiency (E_{mv}):

Now, Peclet number $= N_{Pe} = Z_1^2 / (D_E * q_1)$

Z_1 = length of liquid travel, m

$$D_E = (6.675 * 10^{-3} * (U_a)^{1.44}) + (0.922 * 10^{-4} * h_1) - 0.00562$$

----- (eqⁿ 18.45, page 18.17, 6th edition Perry)

Where D_E = Eddy diffusion coefficient, m²/s

$$D_E = (6.675 * 10^{-3} * (1.232)^{1.44}) + (0.922 * 10^{-4} * 31.662) - 0.00562$$

$$D_E = 0.0063 \text{ m}^2/\text{s}$$

Also,

$$Z_1 = D_c * \cos(\theta_c/2) = 0.87 * \cos(100.73^\circ/2) = 0.555 \text{ m}$$

$$N_{Pe} = Z_1^2 / (D_E * \theta_1)$$

$$= 0.555^2 / (0.0063 * 88.25)$$

$$N_{Pe} = 0.554$$

$$\lambda * E_{og} = 0.4495 * 0.6626 = 0.2978$$

Now, for $\lambda * E_{og} = 0.2978$ and $N_{Pe} = 0.554$

We have from fig.18.29a, page 18.18, 6th edition Perry

$$E_{mv} / E_{og} = 1.09$$

$$E_{mv} = 1.09 * E_{og} = 1.09 * 0.6626 = 0.722$$

$$\text{Murphree Plate Efficiency} = E_{mv} = 0.722$$

3 Overall Efficiency (E_{OC}):

$$\text{Overall Efficiency} = E_{OC} = \frac{\log [1 + E_a (\lambda - 1)]}{\log \lambda}$$

$\log \lambda$

----- (eqⁿ 18.46, page 18.17, 6th edition Perry)

Where, $E_a / E_{mv} = 1 / (1 + E_{MV} [\psi / (1 - \psi)])$

----- (eqⁿ 18.27, page 18.13, 6th edition Perry)

E_{mv} = Murphree Vapor efficiency,

E_a = Murphree Vapor efficiency, corrected for recycle effect of liquid entrainment.

$$(L/G) \cdot \{\rho_g/\rho_l\}^{0.5} = 0.004$$

Thus, for $(L/G) \cdot \{\rho_g/\rho_l\}^{0.5} = 0.004$ and at 80 % of the flooding value,

We have from fig.18.22, page 18.14, 6th edition Perry

ψ = fractional entrainment, moles/mole gross down flow = 0.095

$$\Rightarrow E_\alpha / E_{mv} = 1 / (1 + E_{mv} [\psi / (1 - \psi)])$$

$$\begin{aligned} \Rightarrow E_\alpha &= E_{mv} / (1 + E_{mv} [\psi / (1 - \psi)]) \\ &= 0.722 / (1 + 0.722[0.095 / (1 - 0.095)]) \end{aligned}$$

$$\Rightarrow E_\alpha = 0.6711$$

$$\text{Overall Efficiency} = E_{OC} = \frac{\log [1 + E_\alpha (\lambda - 1)]}{\log \lambda}$$

$$E_{OC} = \log [1 + 0.6711(0.4495 - 1)] / \log 0.4495$$

$$\text{Overall Efficiency} = E_{OC} = 0.5767$$

$$\text{Actual trays} = N_{act} = N_T / E_{OC} = (\text{ideal trays}) / (\text{overall efficiency})$$

Where N_T = Theoretical plates,

N_{act} = actual trays

$$N_{act} = 2 / 0.5767 = 3.47 \approx 4$$

Thus, Actual trays in the Enriching Section = 4

Thus 4th tray is the feed tray.

$$\text{Total Height of Enriching section} = 4 \cdot t_s = 4 \cdot 457 = 1828 \text{ mm} = 1.828 \text{ m} \approx 2 \text{ m.}$$

B) Stripping Section:

1 Point Efficiency, (E_{og}):

$$E_{og} = 1 - e^{-N_{og}} = 1 - \exp(-N_{og}) \text{ ----- (eq}^n \text{ 18.33, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where N_{og} = Overall transfer units

$$N_{og} = 1 / [(1/N_g) + (\lambda/N_l)] \text{ ---- (eq}^n \text{ 18.34, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where N_l = Liquid phase transfer units,

N_g = Gas phase transfer units,

$\lambda = (m \cdot G_m) / L_m$ = Stripping factor,

m = slope of Equilibrium Curve,

G_m = Gas flow rate, mol/s

L_m = Liquid flow rate, mol/s

$$N_g = (0.776 + (0.00457 * h_w) - (0.238 * U_a * \rho_g^{0.5}) + (104.6 * W)) / (N_{Sc, g})^{0.5}$$

----- (eqⁿ 18., page 18., 6th edition Perry)--- *

where h_w = weir height = 50.00 mm

U_a = Gas velocity through active area, m/s

$$= (\text{vapor flow rate in kg/hr}) / (\text{vapor density} \times \text{active area})$$
$$= 1.123 \text{ m/s.}$$

$U_a = 1.123 \text{ m/s}$

$$D_f = (L_w + D_c) / 2 = (0.724 + 0.94) / 2 = 0.832 \text{ m}$$

$$q = 0.00276 \text{ m}^3/\text{s}$$

$$W = \text{Liquid flow rate, m}^3 / (\text{s.m}) \text{ of width of flow path on the plate,}$$
$$= q / D_f = 0.00276 / 0.832 = 0.0033 \text{ m}^3 / (\text{s.m})$$

$$N_{Sc, g} = \text{Schmidt number} = \mu_g / (\rho_g * D_g) = 0.0095 * 10^{-3} / (3.361 * 4.433 * 10^{-6})$$
$$= 0.6776$$

Now,

Number of gas phase transfer units,

$$N_g = (0.776 + (0.00457 * 50) - (0.238 * 1.232 * 3.361^{0.5}) + (105 * 0.0033)) / (0.6776)^{0.5}$$
$$N_g = 1.046$$

Also,

Number of liquid phase transfer units,

$$N_l = k_l * a * \theta_1 \text{----- (eq}^n \text{ 18.36a, page 18.15, 6}^{\text{th}} \text{ edition Perry)}$$

Where, k_l = Liquid phase transfer coefficient kmol/ (sm² kmol/m³) or m/s

a = effective interfacial area for mass transfer m²/m³ froth or spray on the plate,

θ_1 = residence time of liquid in the froth or spray, s

$$\theta_1 = (h_l * A_a) / (1000 * q) \text{---- (eq}^n \text{ 18.38, page 18.16, 6}^{\text{th}} \text{ edition Perry)}$$

now, q = liquid flow rate, m³/s

$$q = 0.00276 \text{ m}^3/\text{s}$$

$$h_l = h_l' = 33.1962 \text{ mm}$$

$$A_a = 0.5208 \text{ m}^2$$

$$\theta_1 = 33.1962 * 0.5208 / (1000 * 0.00276) = 6.264 \text{ s}$$

$$k_1 * a = (3.875 * 10^8 * D_L)^{0.5} * ((0.40 * U_a * \rho_g^{0.5}) + 0.17)$$

--- (eqⁿ. 18.40a, page 18.16, 6th edition Perry)

D_L = liquid phase diffusion coefficient, m²/s

$$k_1 * a = (3.875 * 10^8 * 2.002 * 10^{-9})^{0.5} * ((0.40 * 1.232 * 3.361^{0.5}) + 0.17)$$

$$k_1 * a = 0.875 \text{ m/s}$$

$$N_1 = k_1 * a * \theta_1$$

$$\text{i.e., } N_1 = 0.875 * 6.264 = 5.481 \text{ m}$$

Slope of equilibrium Curve

$$m_{\text{top}} = \underline{0.2}$$

$$m_{\text{bottom}} = \underline{0.3}$$

$$\lambda_t = m_t * G_m / L_m = \underline{2.85}$$

$$\lambda_b = m_b * G_m / L_m = \underline{0.19} \quad \Rightarrow \quad \lambda = 1.52$$

$$N_{og} = 1 / [(1/N_g) + (\lambda/N_1)]$$

$$= 1 / [(1/1.046) + (1.52/5.481)]$$

$$N_{og} = \underline{0.8108}$$

$$E_{og} = 1 - e^{-N_{og}} = 1 - \exp(-N_{og})$$

$$= 1 - e^{-0.8108} = 1 - \exp(-0.8108)$$

$$E_{og} = 0.5555$$

$$\text{Point Efficiency} = E_{og} = \underline{0.5555}$$

2 Murphee Plate Efficiency (E_{mv}):

$$\text{Now, Pelect number} = N_{Pe} = Z_l / (D_E * q_l)$$

Z_l = length of liquid travel, m

$$D_E = (6.675 * 10^{-3} * (U_a)^{1.44}) + (0.922 * 10^{-4} * h_l) - 0.00562$$

----- (eqⁿ. 18.45, page 18.17, 6th edition Perry)

Where, D_E = Eddy diffusion coefficient, m²/s

$$D_E = (6.675 * 10^{-3} * (1.123)^{1.44}) + (0.922 * 10^{-4} * 33.1962) - 0.00562$$

$$D_E = 0.0053 \text{ m}^2/\text{s}$$

Also,

$$Z_l = D_c * \cos(\theta_c/2) = 0.94 * \cos(100.746/2) = 0.5995 \text{ m}$$

$$N_{Pe} = Z_1^2 / (D_E * \theta_l)$$

$$= 0.5995^2 / (0.0053 * 6.264)$$

$$N_{Pe} = 10.82$$

$$\lambda * E_{og} = 1.52 * 0.5555 = 0.844$$

Now for $\lambda * E_{og} = 0.844$ and $N_{Pe} = 10.82$

We have from fig.18.29a, page 18.18, 6th edition Perry

$$E_{mv} / E_{og} = 1.49$$

$$E_{mv} = 1.49 * E_{og} = 1.49 * 0.5555 = 0.8276$$

$$\text{Murphree Plate Efficiency} = E_{mv} = 0.8276$$

3 Overall Efficiency (E_{OC}):

$$\text{Overall Efficiency} = E_{OC} = \frac{\log [1 + E_{\alpha} (\lambda - 1)]}{\log \lambda}$$

----- (eqⁿ. 18.46, page 18.17, 6th edition Perry)

$$\text{where } E_{\alpha} / E_{mv} = 1 / (1 + E_{mv} [\psi / (1 - \psi)])$$

----- (eqⁿ. 18.27, page 18.13, 6th edition Perry)

E_{mv} = Murphee Vapor efficiency,

E_{α} = Murphee Vapor efficiency, corrected for recycle effect of liquid entrainment.

$$(L/G) * \{\rho_g / \rho_l\}^{0.5} = 0.0705$$

thus, for $(L/G) * \{\rho_g / \rho_l\}^{0.5} = 0.0705$ and at 80 % of the flooding value,

we have from fig.18.22, page 18.14, 6th edition Perry

ψ = fractional entrainment, moles/mole gross down flow = 0.04

$$\Rightarrow E_{\alpha} / E_{mv} = 1 / (1 + E_{mv} [\psi / (1 - \psi)])$$

$$\Rightarrow E_{\alpha} = E_{mv} / (1 + E_{mv} [\psi / (1 - \psi)])$$

$$= 0.8276 / (1 + 0.8276 [0.04 / (1 - 0.04)])$$

$$\Rightarrow E_{\alpha} = \underline{0.8}$$

$$\text{Overall Efficiency} = E_{OC} = \frac{\log [1 + E_{\alpha} (\lambda - 1)]}{\log \lambda}$$

$$E_{OC} = \log [1 + 0.8(1.52-1)] / \log 1.52$$

$$\text{Overall Efficiency} = E_{OC} = \underline{0.83}$$

$$\text{Actual trays} = N_{act} = N_T / E_{OC} = (\text{ideal trays}) / (\text{overall efficiency})$$

Where N_T = Theoretical plates,

$$N_{act} = \text{actual trays}$$

$$N_{act} = 2 / 0.83 = 2.41 \approx 3$$

Thus, Actual trays in the Stripping Section = 3

$$\text{Total Height of Stripping section} = 3 * t_s = 3 * 457 = 1371 \text{ mm} = 1.371 \text{ m}$$

$$\begin{aligned} \text{Total Height of Column} = H_C &= \text{Height of Enriching section} + \text{Height of Stripping section} \\ &= 2 + 1.371 = 3.371 \text{ m} \approx 3.4 \text{ m} \end{aligned}$$

SUMMARY OF THE DISTILLATION COLUMN:

A) Enriching section

Tray spacing = 457 mm

Column diameter = 870 mm = 0.87 m

Weir length = 0.67 m

Weir height = 50 mm

Hole diameter = 5 mm

Hole pitch = 15 mm, triangular

Tray thickness = 3 mm

Number of holes = 1971

Flooding % = 80%

B) Stripping section

Tray spacing = 457 mm

Column diameter = 940 mm = 0.94 m

Weir length = 0.724 m

Weir height = 50 mm

Hole diameter = 5 mm

Hole pitch = 15 mm, triangular

Tray thickness = 3 mm

Number of holes = 2308, Flooding % = 80%

5.2 MECHANICAL DESIGN OF DISTILLATION COLUMN:

a) Shell:

Diameter of the tower = $D_i = 940 \text{ mm} = 0.940 \text{ m}$

Working/Operating Pressure = 2.087 atmosphere = 2.1558 kg/cm^2

Design pressure = $1.1 \times \text{Operating Pressure} = 1.1 \times 2.1558 = 2.37138 \text{ kg/cm}^2$

Working temperature = $95 \text{ }^\circ\text{C} = 368 \text{ }^\circ\text{K}$

Design temperature = $104.5 \text{ }^\circ\text{C} = 377.5 \text{ }^\circ\text{K}$

Shell material - IS: 2002-1962 Carbon steel (specific gravity 7.7)

Permissible tensile stress (f_t) = $95 \text{ MN/m}^2 = 970 \text{ kg/cm}^2$

Insulation material - asbestos

Insulation thickness = $2'' = 50.8 \text{ mm}$

Density of insulation = 2700 kg/m^3

Top disengaging space = 0.3 m

Bottom separator space = 0.4 m

Weir height = 50 mm

Down comer clearance = $1'' = 25.4 \text{ mm}$

b) Head - torispherical dished head:

Material - IS: 2002-1962 Carbon steel

Allowable tensile stress = $95 \text{ MN/m}^2 = 970 \text{ kg/cm}^2$

c) Support skirt:

Height of support = 1000 mm = 1.0 m

Material - Carbon Steel

d) Trays-sieve type:

Number of trays = 7

Hole Diameter = 5 mm

Number of holes:

Enriching section = 1971

Stripping section = 2308

Tray spacing:

Enriching section: $18'' = 457 \text{ mm}$

Stripping section: $18'' = 500 \text{ mm}$

Thickness = 3 mm

e) Support for tray:

Purlins - Channels and Angles

Material - Carbon Steel

Permissible Stress = $127.5 \text{ MN/m}^2 = 1299.7 \text{ kgf/cm}^2$

1. Shell minimum thickness:

Considering the vessel as an internal pressure vessel.

$$t_s = ((P \cdot D_i) / ((2 \cdot f_t \cdot J) - P)) + C$$

where t_s = thickness of shell, mm

P = design pressure, kg/cm^2

D_i = diameter of shell, mm

f_t = permissible/allowable tensile stress, kg/cm^2

C = Corrosion allowance, mm

J = Joint factor

Considering double welded butt joint with backing strip

$$J = 85\% = 0.85$$

Thus, $t_s = ((2.37138 \cdot 940) / ((2 \cdot 970 \cdot 0.85) - 2.1558)) + 3 = 4.35 \text{ mm}$

Taking the thickness of the shell = 6 mm (standard)

2. Head Design- Shallow dished and Torispherical head:

Thickness of head = $t_h = (P \cdot R_c \cdot W) / (2 \cdot f \cdot J)$

P = internal design pressure, kg/cm^2

R_c = crown radius = diameter of shell, mm

W = stress intensification factor or stress concentration factor for torispherical head,

$$W = \frac{1}{4} * (3 + (R_c/R_k)^{0.5})$$

R_k = knuckle radius, which is at least 6% of crown radius, mm

Now, $R_c = 940 \text{ mm}$

$$R_k = 6\% \text{ of } R_c = 0.06 \cdot 940 = 56.4 \text{ mm}$$

$$W = \frac{1}{4} * (3 + (R_c/R_k)^{0.5}) = \frac{1}{4} * (3 + (940/56.4)^{0.5}) = 1.7706 \text{ mm}$$

$$t_h = (2.37138 * 940 * 1.7706) / (2 * 970 * 0.85) = 2.39 \text{ mm}$$

Including corrosion allowance take the thickness of head = 6 mm

Weight of Head:

$$\text{Diameter} = \text{O.D} + (\text{O.D}/24) + (2 * s_f) + (2 * i_{cr}/3) \text{ --- (eq}^n \text{ 5.12 Brownell and Young)}$$

Where O.D. = Outer diameter of the dish, inch

i_{cr} = inside cover radius, inch

s_f = straight flange length, inch

From table 5.7 and 5.8 of Brownell and Young

$$s_f = 1.5''$$

$$i_{cr} = 2.31''$$

Also, O.D. = 940 mm = 37''

$$\text{Diameter} = 37 + (37/24) + (2 * 1.5) + (2/3 * 2.31)$$

$$d = 43.08'' = 1094.23 \text{ mm.}$$

$$\text{Weight of Head} = ((\pi * d^2 * t) / 4) * (\rho / 1728)$$

$$= ((\pi * 43.08^2 * 0.2362) / 4) * (7700 / 1728) = 1534.15 \text{ lb}$$

$$= 695.87 \text{ kg}$$

3. Shell thickness at different heights

At a distance 'X' m from the top of the shell the stresses are:

3.1 Axial Tensile Stress due to Pressure:

$$f_{ap} = \frac{P * D_i}{4(t_s - c)} = \frac{2.37138 * 940}{4(6 - 3)} = 185.758 \text{ kgf/cm}^2 .$$

This is the same through out the column height.

3.2 Circumferential stress

$$2 * f_{ap} = 2 * 185.758 = 371.516 \text{ kgf/cm}^2$$

3.3 Compressive stress due Dead Loads:

3.3.1 Compressive stress due to Weight of shell up to a distance 'X' meter from top.

$$f_{ds} = \text{weight of shell/cross-section of shell}$$

$$= (\pi/4) * (D_o^2 - D_i^2) * \rho_s * X / (\pi/4) * (D_o^2 - D_i^2)$$

$$= \text{weight of shell per unit height } X / (\pi * D_m * (t_s - c))$$

Where D_o and D_i are external and internal diameter of shell.

$$\rho_s = \text{density of shell material, kg/m}^3$$

$$D_m = \text{mean diameter of shell,}$$

$$t_s = \text{thickness of shell,}$$

$$c = \text{corrosion allowance}$$

$$\text{Now, } \rho_s = 7700 \text{ kg/m}^3 = 0.0077 \text{ kg/cm}^3$$

$$f_{ds} = \rho_s * X = (7700 * X) \text{ kg/m}^2 = (0.77 * X) \text{ kg/cm}^2$$

The vessel contains manholes, nozzles etc., additional weight may be estimated 20% of the weight of the shell.

$$f_{T,ds} = 1.2 * 7700 * X = 0.924 * (X) \text{ kg/cm}^2$$

3.3.2 Compressive stress due to weight of insulation at a height X meter:

$$f_{d(ins)} = \frac{\pi * D_{ins} * t_{ins} * \rho_{ins} * X}{\pi * D_m * (t_s - c)} = \frac{\text{weight of insulation per unit height (X)}}{\pi * D_m * (t_s - c)}$$

where D_{ins} , t_{ins} , ρ_{ins} are diameter, thickness and density of insulation respectively.

$$D_m = (D_c + (D_c + 2t_s)) / 2$$

Assuming asbestos is to be used as insulation material.

$$\rho_{ins} = 2700 \text{ kg/m}^3$$

$$t_{ins} = 2'' = 5.08 \text{ cm.}$$

$$D_{ins} = D_c + 2t_s + 2t_{ins} = 94 + (2 * 0.6) + (2 * 5.08) = 105.36 \text{ cm.}$$

$$D_m = (94 + (94 + (2 * 0.6))) / 2 = 94.60 \text{ cm.}$$

$$f_{d(ins)} = \frac{\pi * 105.36 * 5.08 * 2700 * X}{\pi * 94.6 * (0.6 - 0.3)} = 50920.28 * X \text{ kg/m}^2$$

$$= 5.092028 * X \text{ kg/cm}^3$$

3.3.3 Stress due to the weight of the liquid and tray in the column up to a height X meter.

$$f_{d, liq.} = \frac{\sum \text{weight of liquid and tray per unit height } X}{\pi * D_m * (t_s - c)}$$

The top chamber height is 0.3 m and it does not contain any liquid or tray. Tray

spacing is 457 mm.

Average liquid density = 775.45 kg/m³

Liquid and tray weight for X meter

$$\begin{aligned}
 F_{\text{liq-tray}} &= [(X-0.3)/0.5 + 1] * (\pi * D_i^2/4) * \rho_l \\
 &= [(X-0.3)/0.5 + 1] * (\pi * 0.94^2/4) * 775.4 \\
 &= [2X + 0.4] * 538.11 \text{ kg} \\
 f_{\text{d (liq)}} &= F_{\text{liq-tray}} * 10 / (\pi * D_m * (t_s - c)) \\
 &= [2X + 0.4] * 538.11 * 10 / (\pi * 946 * (6 - 3)) \\
 &= [2X + 0.4] * 0.6035 \\
 &= 1.207 * X + 0.2414 \text{ kg/cm}^2
 \end{aligned}$$

3.3.4 Compressive stress due to attachments such as internals, top head, platforms and ladder up to height X meter.

$$f_{\text{d (attach.)}} = \frac{\sum \text{weight of attachments per unit height } X}{\pi * D_m * (t_s - c)}$$

Now total weight up to height X meter = weight of top head + pipes + ladder, etc.,

Taking the weight of pipes, ladder and platforms as 25 kg/m = 0.25 kg/cm

Total weight up to height X meter = (695.87+25X) kg

$$f_{\text{d (attach.)}} = (695.87+25X) * 10 / \pi * 946 * (6 - 3) = 0.7805 + 0.028X \text{ kg/cm}^2$$

Total compressive dead weight stress:

$$\begin{aligned}
 f_{\text{dx}} &= f_{\text{ds}} + f_{\text{ins}} + f_{\text{d (liq)}} + f_{\text{d (attach)}} \\
 &= 0.924X + 5.092X + [1.207X+0.2414] + [0.7805 + 0.028X] \\
 f_{\text{dx}} &= 7.251X + 1.0219 \text{ kg/cm}^2
 \end{aligned}$$

4. Tensile stress due to wind load in self supporting vessels:

$$f_{\text{wx}} = M_w / Z$$

Where, M_w = bending moment due to wind load = (wind load * distance)/2

$$= 0.7 * P_w * D * X^2 / 2$$

Z = modulus for the section for the area of shell $\approx \pi * D_m^2 * (t_s - c) / 4$

Thus, $f_{\text{wx}} = 1.4 * P_w * X^2 / (\pi * D_m * (t_s - c))$

Now $P_w = 25 \text{ lb/ft}^2$ --- (from table 9.1 Brownell and Young)

$$= 37.204 \text{ kg/m}^2$$

Bending moment due to wind load

$$M_{wx} = 0.7 * 37.204 * 0.94 * X^2 / 2 = 12.24(X^2) \text{ kg-m}$$

$$f_{wx} = 1.4 * 37.204 * X^2 / (\pi * 0.94 * (6-3) * 10^{-3}) = 0.58792(X^2) \text{ kg/cm}^2$$

5. Stresses due to Seismic load:

$$f_{sx} = M_{sx} / (\pi * D_m^2 * (t_s - c) / 4)$$

Where, bending moment M_{sx} at a distance X meter is given by

$$M_{sx} = [C * W * X^2 / 3] * [(3H - X) / H^2]$$

Where, C = seismic coefficient,

W = total weight of column, kg

H = height of column

$$\text{Total weight of column} = W = C_v * \pi * \rho_m * D_m * g * (H_v + (0.8 * D_m)) * t_s * 10^{-3}$$

----- (eqⁿ 13.75, page 743, Coulson and Richardson 6th volume)

Where W = total weight of column, excluding the internal fittings like plates, N

C_v = a factor to account for the weight of nozzles, man ways, internal supports, etc.

= 1.5 for distillation column with several man ways, and with plate support rings or equivalent fittings

H_v = height or length between tangent lines (length of cylindrical section)

g = gravitational acceleration = 9.81 m/s²

t = wall thickness

ρ_m = density of vessel material, kg/m³

D_m = mean diameter of vessel = $D_i + (t * 10^{-3}) = 0.94 + (6 * 10^{-3}) = 0.946 \text{ m}$

$$W = 1.5 * \pi * 7700 * 0.946 * 9.81 * (3.0 + (0.8 * 0.946)) * 6 * 10^{-3} = 7590.341 \text{ N} = 773.73 \text{ kg.}$$

Weight of plates: ----- (Coulson and Richardson 6th volume)

$$\text{Plate area} = \pi * 0.94^2 / 4 = 0.694 \text{ m}^2$$

$$\text{Weight of each plate} = 1.2 * 0.694 = 0.8328 \text{ kN}$$

$$\text{Weight of 7 plates} = 7 * 0.8328 = 5.8296 \text{ kN} = 594.25 \text{ kg.}$$

$$\text{Total weight of column} = 773.73 + 594.25 = 1367.98 \text{ kg.}$$

Let, C = seismic coefficient = 0.08

$$M_{sx} = [0.08 * 1367.98 * X^2 / 3] * [((3 * 3.4) - X) / 3.4^2]$$

$$\begin{aligned}
&= 36.48X^2 * [0.8823-0.086X] \text{ kg-m} \\
f_{sx} &= M_{sx} * 10^3 / (\pi * D_m^2 * (t_s - c) / 4) \\
&= 36.48X^2 * [0.8823 - 0.086X * 10^3 / (\pi * 94.6^2 * (6-3) / 4)] \\
&= [1.526X^2 - 0.14878X^3], \text{ kg/cm}^2
\end{aligned}$$

On the up wind side:

$$f_{t,max} = (f_{wx} \text{ or } f_{sx}) + f_{ap} - f_{dx}$$

Since the chances of, stresses due to wind load and seismic load, to occur together is rare hence it is assumed that the stresses due to wind load and earthquake load will not occur simultaneously and hence the maximum value of either is therefore accepted and considered for evaluation of combined stresses.

Thus,

$$\begin{aligned}
f_{t,max} &= 0.58792X^2 + 168.871 - [7.215X + 1.0129] \\
\text{i.e., } &0.58792X^2 - 7.251X + 168.871 - 1.0129 - 824.5 = 0 \\
&0.58792X^2 - 7.251X - 656.64 = 0 \\
\Rightarrow &X = 40.15 \text{ m}
\end{aligned}$$

On the down side:

$$\begin{aligned}
f_{c,max} &= (f_{wx} \text{ or } f_{sx}) - f_{ap} + f_{dx} \\
3.075X^2 - 86.1618 + [7.3580X + 0.6701] &= f_{c,max} \\
\text{The column height is 3.4 m, for which the maximum value is} \\
f_{c,max} &= 0.58792(3.4)^2 - 168.871 + [7.251(3.4) + 1.0129] \\
&= \underline{-136.408} \text{ kg/cm}^2
\end{aligned}$$

this shows that the stress on the down wind side is tensile.

$$\begin{aligned}
f_{t,max} &= 85\% \text{ of allowable tensile stress.} \\
f_{t,max} &= 970 * 0.85 = 824.5 \text{ kg/cm}^2 \\
f_{t,max} &= 0.58792(X)^2 - 168.871 + [7.251(X) + 1.0129] = 824.5 \\
\text{Therefore, } &X = 35.38 \text{ m.}
\end{aligned}$$

Hence we see that the design value of the column height is more than 3.4 m, which is the actual column height. So we conclude that the design is safe and thus the design calculations are acceptable.

Hence a thickness of 6 mm is taken throughout the length of shell.

$$\text{Height of the head} = D_c / 4 = 0.94 / 4 = 0.235 \text{ m}$$

Skirt support Height = 1.0 m

Total actual height = 3.4 + 1 + 0.235 = 4.635 m

5.2.1 Design of Support:

a) Skirt Support:

The cylindrical shell of the skirt is designed for the combination of stresses due to vessel dead weight, wind load and seismic load. The thickness of skirt is uniform and is designed to withstand maximum values of tensile or compressive stresses.

Data available:

- (i) Diameter = 940 mm.
- (ii) Height = 3400 mm = 3.40 m
- (iii) Weight of vessel, attachment = 2148.85 kg.
- (iv) Diameter of skirt (straight) = 940 mm
- (v) Height of skirt = 1.0 m
- (vi) Wind pressure = 37.204 kg/m²

1. Stresses due to dead Weight:

$$f_d = \sum W / (\pi * D_{ok} * t_{sk})$$

f_d = stress,

$\sum W$ = dead weight of vessel contents and attachments,

D_{ok} = outside diameter of skirt,

t_{sk} = thickness of skirt,

$$f_d = 2148.85 / (\pi * 95.2 * t_{sk}) = 7.1848 / t_{sk} \text{ kg/cm}^2$$

2. Stress due to wind load:

$$p_w = k * p_1 * h_1 * D_o$$

p_1 = wind pressure for the lower part of vessel,

k = coefficient depending on the shape factor

= 0.7 for cylindrical vessel.

D_o = outside diameter of vessel,

The bending moment due to wind at the base of the vessel is given by

$$M_w = p_w * H/2$$

$$f_{wb} = M_w/Z = 4 * M_w/(\pi * (D_{ok})^2 * t_{sk})$$

Z- Modulus of section of skirt cross-section

$$p_w = 0.7 * 37.204 * 1.0 * 0.9 = 120.785 \text{ kg}$$

$$M_w = p_w * H/2 = 120.795 * 10/2 = 603.975 \text{ kg-m}$$

Substituting the values we get,

$$f_{wb} = 708.4737/t_{sk} \text{ kg/cm}^2$$

3. Stress due to seismic load:

$$\text{Load} = C * W$$

C = seismic coefficient,

W = total weight of column.

$$\text{Stress at base, } f_{sb} = (2/3) * (C * H * W) / (\pi * (R_{ok})^2 * t_{sk})$$

$$C = 0.08$$

$$f_{sb} = (2/3) * (0.08 * 2148.85 * 340) / (\pi * (95.2/2)^2 * t_{sk}) = 0.5474 / t_{sk} \text{ kg/cm}^2$$

Maximum tensile stress:

$$f_{t, \max} = (8.9458 / t_{sk}) - (7.1848 / t_{sk}) = (1.761 / t_{sk}) \text{ kg/cm}^2$$

$$\text{Permissible tensile stress} = 925 \text{ kg/cm}^2$$

$$\text{Thus, } 925 = (1.761 / t_{sk})$$

$$\Rightarrow t_{sk} = 1.761/925 = 0.0019 \text{ cm} = 0.019 \text{ mm}$$

Maximum compressive stress:

$$f_{c, \max} = (8.9458 / t_{sk}) + (7.1848 / t_{sk}) = (16.1306 / t_{sk}) \text{ kg/cm}^2$$

Now,

$$f_{c, (\text{permissible})} \leq (1/3) \text{ yield point}$$

$$= 1500 / 3 = 500 \text{ kg/cm}^2$$

$$\text{Thus, } t_{sk} = 16.1306/500 = 0.03 \text{ cm} = 0.3 \text{ mm}$$

As per IS 2825-1969, minimum corroded skirt thickness = 7 mm

Thus use a thickness of 7 mm for the skirt.

Design of skirt bearing plate:

Assume both circle diameter = skirt diameter + 32.5 = 94 + 32.5 = 126.5 cm

Compressive stress between Bearing plate and concrete foundation:

$$f_c = (\sum W/A) + (M_w/Z)$$

$\sum W$ = dead weight of vessel contents and attachments,

A = area of contact between the bearing plate and foundation,

Z = Section Modulus of area,

M_w = the bending moment due to wind,

$$f_c = (2148.85 * 4) / (\pi * (126.5^2 - 94^2)) + (0.7 * 37.204 * 3 * 42.3^2) / (2 * \pi * (126.5^4 - 94^4) / (32 * 126.5))$$
$$= 0.0954 + 0.506$$

$$f_c = 0.6014 \text{ kg/cm}^2$$

Which is less than the permissible value for concrete.

Maximum bending moment in bearing plate

$$M_{\max} = (0.6014 * 16.25^2 / 2) = 79.4 \text{ kg-cm}$$

$$\text{Stress, } f = (6 * 0.6014 * 16.25^2) / (2 * t_B^2) = 476.42 / t_B^2$$

Permissible stress in bending is 1000 kg/cm²

$$\text{Thus, } t_B^2 = 476.42 / 1000 \Rightarrow t_B = 0.6902 \text{ cm} = 6.902 \text{ mm}$$

Therefore, a bolted chair has to be used.

Anchor Bolts:

Minimum weight of Vessel = $W_{\min} = 1400 \text{ kg}$. ----- (assumed value)

$$f_{c,\min} = (W_{\min}/A) - (M_w/Z)$$

$$= [(4 * 1400) / (\pi * (126.5^2 - 94^2))] - (0.7 * 37.204 * 3 * 42.3^2) / (2 * \pi * (126.5^4 - 94^4) / (32 * 126.5))$$
$$= 0.2487 - 0.5059 = -0.2572 \text{ kg/cm}^2$$

Since f_c is negative, the vessel skirt must be anchored to the concrete foundation by

anchor bolts.

Assuming there are 24 bolts,

$$P_{\text{bolts}} = (0.2572/24) * ((\pi * (126.5^2 - 94^2))/4) = 19.199 \text{ kg}$$

Trays:

The trays are standard sieve plates throughout the column. The plates have 1971 holes in Enriching section and 2308 holes in the Stripping section of 5mm diameter arranged on a 15mm triangular pitch. The trays are supported on purloins.

5.2.2 Nozzle Design:

Nozzles are required for compensation where a hole is made in the shell. The following nozzles are required:

1. Feed Nozzle:

$$\text{Liquid Velocity} = V_L = 2 \text{ m/s}$$

$$\text{Area of Nozzle} = (\text{Mass of liquid in}) / (\rho_L * V_L)$$

$$\begin{aligned} \text{Mass of liquid in} &= 6741.976 \text{ kg/hr.} \\ &= 1.87277 \text{ kg/s} \end{aligned}$$

$$\text{Thus, Area of Nozzle} = (1.87277) / (784.50 * 2) = 1.1936 \times 10^{-3} \text{ m}^2$$

$$\text{Now, Area of Nozzle} = \pi * d_N^2 / 4 = 1.1936 * 10^{-3} \text{ m}^2$$

$$d_N^2 = (4 * 1.1936 * 10^{-3} / \pi)$$

$$d_N = 0.03898 \text{ m} = 38.98 \text{ mm.}$$

2. Nozzle for distillate:

$$\text{Gas Velocity} = V_G = 25.0 \text{ m/s}$$

$$\text{Area of Nozzle} = (\text{Mass of liquid in}) / (\rho_G * V_G)$$

$$\begin{aligned} \text{Mass of vapor in} &= 6372.56 \text{ kg/hr.} \\ &= 1.77 \text{ kg/s} \end{aligned}$$

$$\text{Thus, Area of Nozzle} = (1.77) / (3.4376 * 25) = 0.0206 \text{ m}^2$$

$$\text{Now, Area of Nozzle} = \pi * d_N^2 / 4 = 0.0206 \text{ m}^2$$

$$d_N^2 = (4 * 0.0206 / \pi)$$

$$d_N = 0.1619 \text{ m} = 16.19 \text{ cm.}$$

3. Nozzle for residue:

$$\text{Liquid Velocity} = V_L = 1.0 \text{ m/s}$$

$$\text{Area of Nozzle} = (\text{Mass of liquid in}) / (\rho_L * V_L)$$

$$\begin{aligned} \text{Mass of liquid in} &= 369.416 \text{ kg/hr.} \\ &= 0.1026 \text{ kg/s} \end{aligned}$$

$$\text{Thus, Area of Nozzle} = (0.1026) / (784.87 * 1) = 1.3072 * 10^{-4} \text{ m}^2$$

$$\text{Now, Area of Nozzle} = \pi * d_N^2 / 4 = 1.3072 \text{ m}^2$$

$$d_N^2 = (4 * 1.3072 * 10^{-4} / \pi)$$

$$d_N = 0.0129 \text{ m} = 12.9 \text{ mm.}$$

5.3 Process Design of Heat exchanger

Heat exchanger used is shell and tube.

The ethanol entering from vaporizer must be heated from 100°C to 200°C using ethanol, acetaldehyde and hydrogen mixture available at 310°C.

Shell side:

$$\text{Feed } (m_h) = 2.008 \text{ kg/sec}$$

$$\text{Inlet temperature } (T1) = 100^\circ\text{C}$$

$$\text{Outlet temperature } (T2) = 200^\circ\text{C}$$

Tube side:

$$\text{Inlet temperature } (t1) = 310^\circ\text{C}$$

$$\text{Outlet temperature } (t2) = 232.690^\circ\text{C}$$

1) Heat balance

$$\begin{aligned} Q_h &= m_h C_p (T2 - T1) \\ &= 2.008 * 1.97 * (200 - 100) \\ &= 395.576 \text{ KW} \end{aligned}$$

2) LMTD

$$\text{LMTD}=120.99^{\circ}\text{C}$$

F_T =LMTD correction factor.

$$R=0.7731 \text{ \& } S=0.476$$

From graph of F_T Vs S

$$F_T =0.91$$

$$\text{LMTD (corrected)}= 110.1009^{\circ}\text{C}.$$

3) Heat transfer area:

Choose overall heat transfer coefficient= 120 W/(m²K)

$$Q = UA(\text{LMTD})$$

$$A=395576 / (120*120.99*0.91)$$

$$A=29.94\text{m}^2$$

4) Tube selection:

¾ in OD ,10 BWG Tubes

$$\text{OD}=3/4 \text{ in}=19.05 \text{ mm}$$

$$\text{ID}=0.685 \text{ in}=17.399 \text{ mm}$$

$$\text{Length of tube } =L=16\text{ft}=4.88\text{m}$$

$$\text{Heat transfer area per tube } =0.292 \text{ m}^2$$

$$\text{Number of tubes}= 29.94/0.292=102.53$$

TEMA P or S, Floating head type:

Nearest tube count from tube count table

$$N_T= 102$$

2 tube passes and 1 shell pass

¾ in tubes arranged in triangular pitch

$$\text{Shell ID } (D_f)=305\text{mm}=12\text{in}$$

$$\text{Corrected heat transfer area}=0.292*102=29.784 \text{ m}^2$$

$$\text{Corrected over all heat transfer coefficient } (U)=120.63 \text{ W}/(\text{m}^2\text{K})$$

5) Average properties of fluids

a) Shell side (ammoniated brine) at 150°C

$$\rho=3.98 \text{ kg/m}^3$$

$$\mu=1300 \cdot 10^{-8} \text{ mNs/m}^2$$

$$C_p=1.97 \text{ KJ/kg.K}$$

$$k=0.0256 \text{ w/m.k}$$

b) Tube side (water) at 25⁰C

$$\rho=2.965 \text{ kg/m}^3$$

$$\mu=4.7577 \cdot 10^{-5} \text{ mNs/m}^2$$

$$C_p=1.7117 \text{ KJ/kg.K}$$

$$k=0.081 \text{ w/m.k}$$

6) Tube side velocity

Number of passes $N_p=2$

$$\text{Flow area} = (\pi \cdot ID^2/4) \cdot N_T/N_p$$

$$= (3.14 \cdot 0.017399^2/4) \cdot 102/2$$

$$A_a=0.012 \text{ m}^2$$

$$V_t=m_c / (A_a \rho)$$

$$=2.008 / (0.012 \cdot 2.965)$$

$$=56.43 \text{ m/s.}$$

Velocity is with the range (for vapor

7) Shell side velocity

$$S_m=[(P^1-D_o)L_s]D_s/P^1$$

$S_m \rightarrow$ cross flow area at center of shell.

$N_b \rightarrow$ Number of baffles.

$L \rightarrow$ Tube length.

$(P^1-D_o) \cdot L_s \rightarrow$ Flow area between two adjacent tube rows.

$D_s/P^1 \rightarrow$ Number of tube rows.

$$S_m = [(25.4-19.05) \cdot 244] \cdot 305/25.4$$

$$=0.018605 \text{ m}^2.$$

$$V_s=m_h / (\rho S_m)$$

$$=2.008 / (3.8 \cdot 0.018605)$$

$$=28.4 \text{ m/s}$$

$$P^1 = 25.4 \text{ mm.}$$

$$L_s = 0.8 \cdot D_s$$

$$= 0.244 \text{ m.}$$

$$N_{b+1} = L/L_S$$

$$= 4.88/0.244$$

$$N_b = 19 \text{ baffles}$$

8) Shell side heat transfer coefficient:

$$N_{NU} = j_H N_{Re} (N_{Pr})^{1/3}$$

N_{Nu} = nusselt number

$$N_{Re} = V_s D_o \rho / \mu$$

N_{Re} = Reynolds number

$$= 28.40 * 19.05 * 10^{-3} * 3.98 / (1300 * 10^{-8})$$

$$= 165635$$

$$j_h = 3 * 10^{-3}$$

$$N_{Pr} = \mu C_p / k$$

$$= 1300 * 10^{-8} * 1.97 / (2.855 * 10^{-4}) = 0.09$$

$$N_{NU} = 3 * 10^{-3} * 165635 * 0.09^{0.33} = 222.68$$

$$h_o = 222.68 * 0.0256 / 0.01905 = 299.244 \text{ W / m}^2 \text{ K.}$$

9) Tube side heat transfer coefficient:

$$N_{Nu} = 0.023 (N_{Re})^{0.8} (N_{Pr})^{0.3}$$

$$N_{Re} = 61187.4$$

$$N_{Pr} = 0.796$$

$$N_{Nu} = 0.023 (61187.4)^{0.8} (0.796)^{0.3} = 226.82$$

$$h_i = 1055.9 \text{ w/m}^2 \cdot \text{K}$$

10) Overall heat transfer coefficient:

$$\text{Dirt coefficient} = 3.522 * 10^{-4} \text{ w/m}^2 \cdot \text{K}$$

$$1/U = 1/h_o + (D_o/D_i)(1/h_i) + D_o \ln(D_o/D_i) / (2 * K_w) + \text{dirt coefficient}$$

$$1/U = 1/299.24 + (19.05/17.399)(1/1055.9) + 0.01905 * \ln(19.05/17.399) / (2 * 50) + 3.522 * 10^{-4}$$

$$U = 210.608 \text{ w/m}^2 \cdot \text{K}$$

Designed value is greater than the assumed value.

11) Pressure drop calculation:

11a) Tube side pressure drop:

Tube side Reynolds number= $N_{Re}= 61187.4$

Friction factor= $f=0.079(N_{Re})^{-1/4} = 0.079(61187.4)^{-1/4} = 5.023*10^{-3}$

$$\Delta P_L = (4fL v_t^2 / 2gD_i) * \rho_t g$$

$$= (4 * 5.023 * 10^{-3} * 4.88 * 56.43^2 / 2 * 9.8 * 17.399 * 10^{-3}) * 2.965 * 9.8$$

$$= 20603.08 \text{ N/m}^2$$

$$\Delta P_E = 2.5(\rho_t v_t^2 / 2)$$

$$= 2.5(2.965 * 56.43^2 / 2)$$

$$= 11802 \text{ N/m}^2$$

$$(\Delta P)_T = N_p(\Delta P_L + \Delta P_E)$$

$$= 2 * (20603.08 + 11802) = 64810 \text{ N/m}^2 = 64.810 \text{ kPa.}$$

11b) Shell side pressure drop (Bell's method):

Shell side Reynolds number= $N_{Re}=165635$

$$f_k = 0.1$$

Pressure drop for cross flow zones

$$\Delta P_C = (b f_k w^2 N_C / \rho_f S_m^2) (\mu_w / \mu_f)$$

N_C = number of tube rows crossed in one cross flow section.

$$N_C = D_s [1 - 2(L_C / D_s)] / P_P$$

Where, L_C baffle cut, 25% of D_s

$$P_P = ((\sqrt{3}) / 2) P^I$$

$$N_C = 0.305 * [1 - 2 * 0.5] / 0.022$$

$$N_C = 7$$

$$\Delta P_C = (2 * 10^{-3} * 0.1 * 2.008^2 * 7) / (3.98 * 0.018605^2)$$

$$\Delta P_C = 0.076 \text{ K Pa}$$

Pressure drop in end zones:

$$\Delta P_E = \Delta P_C (1 + N_{cw} / N_C)$$

$N_{cw} = 0.8 L_C / P_P$, number of cross flow rows in each window.

$$N_{cw} = 3$$

$$\Delta P_E = 0.076 * (1 + 3/7)$$

$$\Delta P_E = 0.10857 \text{ kPa.}$$

Pressure drop in window zones:

$$\Delta P_w = b w^2 (2 + 0.6 N_{cw}) / (S_m S_w \rho)$$

$$S_w = S_{wg} - S_{wt}$$

S_w = area for flow through window zone.

S_{wg} = gross window area

S_{wt} = area occupied by tubes

$$S_{wg} = 25 \text{ in}^2 = 0.01613 \text{ m}^2, \text{ for } D_s = 12 \text{ in} \ \& \ L_c/D_s = 0.25$$

$$S_{wt} = (N_T/8)(1 - F_C) \Pi D_o^2$$

$$F_C = 0.63 \text{ for } L_c/D_s = 0.25$$

$$S_{wt} = (102/8)(1 - 0.63) * \Pi * 0.01905^2$$

$$S_{wt} = 5.378 * 10^{-3} \text{ m}^2.$$

$$S_w = (0.01613 - 5.378 * 10^{-3}) = 0.010752 \text{ m}^2$$

$$\Delta P_w = \frac{5 * 10^{-5} * 2.008^2 * (2 + 0.6 * 8)}{0.018605 * 0.010752 * 3.98}$$

$$\Delta P_w = 0.962 \text{ kPa}$$

$$(\Delta P_s)_T = 2 \Delta P_E + (N_b - 1) \Delta P_C + N_b \Delta P_w$$

$$(\Delta P_s)_T = 2 * 1.69 + (8 - 1) * 1.19 + 8 * 1.127$$

$$(\Delta P_s)_T = 21.8174 \text{ kPa}$$

5.4 Mechanical design of Heat Exchanger:**(a) Shell side details:**

Material: carbon steel

Number of shell passes: one

Working pressure: 0.3 N/mm²

Design pressure: 0.33 N/mm²

Inlet temperature: 100⁰C

Out let temperature: 200⁰C

Permissible stress for carbon steel: 95 N/mm²

(b) Tube side details:

Number tubes: 102

Number of passes: 2

Outside diameter: 19.05mm
Inside diameter: 17.399 mm.
Length: 4.88m
Pitch triangular: 1 inch
Working pressure: 0.3 N/mm²
Design pressure: 0.33N/mm²
Inlet temperature: 310⁰C
Outlet temperature: 232.69⁰C

Shell side:

(1) Shell thickness:

$$t_s = PD / (2fJ + P)$$
$$= 0.33 * 305 / (2 * 95 * 0.85 + 0.33) = 0.57$$

Minimum thickness of shell must be = 6.0 mm

Including corrosion allowance shell thickness is 8mm

(2) Head thickness:

Shallow dished and torispherical

$$t_s = PR_c W / 2fJ$$
$$= 0.33 * 305 * 1.77 / (2 * 95 * 0.85)$$
$$= 1.103 \text{ mm.}$$

Minimum shell thickness should be 10mm including corrosion allowance.

(3) Transverse Baffles:

Baffle spacing = 0.8 * D_c = 244mm

Number of baffles,

$$N_b + 1 = L / L_s = 4.88 / 0.244 = 20$$

$$N_b = 19$$

Thickness of baffles, t_b = 6mm

(4) Tie Rods and spacers

For shell diameter, 300-500mm

Diameter of Rod = 9mm

Number of rods = 4

(5) Flanges

Design pressure = 0.33 N/mm^2

Flange material IS: 2004-1962, class 2

Bolting steel: 5% Cr-Mo steel

Gasket material: asbestos composition

Shell thickness: $8 \text{ mm} = g_o$

Outside diameter of shell: 305 mm

Allowable stress of flange material: 100 MN/m^2

Allowable stress of bolting material = 138 MN/m^2

Shell thickness = 10 mm.

Outside diameter = 325 mm.

Determination of gasket width:

$$d_o/d_i = [(y - Pm)/(y - P(m+1))]^{0.5}$$

Assume a gasket thickness of 10 mm

y = minimum design yield seating stress = 25.5 MN/m^2

m = gasket factor = 2.75

$$d_o/d_i = [(25.5 - 0.33 * 2.75)/(25.5 - 0.33(2.75 + 1))]^{0.5}$$

$$d_o/d_i = 1.0067$$

Let, d_i of gasket equal 335 mm

$$d_o = 1.002 * d_i$$

$$d_o = 0.33724 \text{ m}$$

Minimum gasket width = $(337.24 - 335)/2 = 1.12 \text{ mm} = 0.00112 \text{ m}$.

Taking gasket width of $N = 0.010 \text{ m}$

$$d_o = 0.35924 \text{ m}.$$

Basic gasket seating width, $b_o = 5 \text{ mm}$

Diameter of location of gasket load reaction is

$$G = d_i + N = 0.335 + 0.01 = 0.345 \text{ m}$$

Estimation of Bolt loads:

Load due to design pressure

$$H = \pi G^2 P / 4 = 3.14 * 0.345^2 * 0.33 / 4 = 0.03085 \text{ MN}$$

Load to keep joint tight under operation

$$b = 2.5 (b_0)^{0.5} = 5.59 \text{ mm.}$$

$$H_p = \pi * G * (2b) * m * p = 3.14 * 0.345 * (2 * 0.00559) * 2.75 * 0.33 = 0.011 \text{ MN}$$

Total operating load,

$$W_o = H + H_p = 0.03085 + 0.011 = 0.04185 \text{ MN.}$$

Load to seat gasket under bolting condition

$$W_g = \pi * G * b * y = 3.14 * 0.345 * 5.59 * 10^{-3} * 25.5 = 0.1545 \text{ MN.}$$

$$W_g > W_o, \text{ controlling load} = 0.1545 \text{ MN}$$

Calculation of optimum bolting area:

$$A_m = A_g = W_g / S_g = 0.1545 / 138 = 1.12 * 10^{-3} \text{ m}^2$$

Calculation of optimum bolt size:

Bolt size, M18 X 2

Actual number of bolts = 20

Radial clearance from bolt circle to point of connection of hub or nozzle and back of flange = R = 0.027 m

$$C = ID + 2(1.415g + R) = 325 + 2[11.315 + 0.027 * 10^3] = 401.63 \text{ mm} = 0.40163$$

Bolt circle diameter = 0.40163 m.

Calculation of flange outside diameter

Let, bolt diameter = 18 mm.

$$A = C + \text{bolt diameter} + 0.02 = 0.40163 + 0.018 + 0.02 = 0.43963 \text{ m.}$$

Check for gasket width,

$$A_b S_G / (\pi G N) = 1.54 * 10^{-4} * 20 * 138 / (3.14 * 0.345 * 10^{-2}) = 39.21 < 2 * y.$$

Where, S_G is the Allowable stress for the gasket material.

Flange moment computation:

(a) For operating condition

$$W_o = W_1 + W_2 + W_3$$

$$W_1 = \pi * B^2 * P / 4 = \pi * 0.325^2 * 0.33 / 4 = 0.027 \text{ MN}$$

$$W_2 = H - W_1 = 0.03085 - 0.027 = 0.00385 \text{ MN.}$$

$$W_3 = W_0 - H = H_p = 0.011 \text{ MN.}$$

M_0 = Total flange moment

$$M_0 = W_1 a_1 + W_2 a_2 + W_3 a_3$$

$$a_1 = (C - B) / 2 = (0.40163 - 0.325) / 2$$

$$a_1 = 0.038315 \text{ m}$$

$$a_3 = (C - G) / 2 = (0.40163 - 0.345) / 2$$

$$a_3 = 0.028315 \text{ m}$$

$$a_2 = (a_1 + a_3) / 2 = (0.038315 + 0.028315) / 2 = 0.033315 \text{ m}$$

$$M_0 = 0.027 * 0.038315 + 0.00385 * 0.033315 + 0.011 * 0.028315$$

$$M_0 = 1.474 * 10^{-3} \text{ MN-m}$$

(b) For bolting condition

$$M_g = W a_3$$

$$W = (A_m + A_b) * S_g / 2$$

$$A_b = 20 * 1.54 * 10^{-4} = 3.08 * 10^{-3} \text{ m}^2$$

$$A_m = 1.12 * 10^{-3} \text{ m}^2$$

$$W = (1.12 * 10^{-3} + 3.08 * 10^{-3}) * 138 / 2$$

$$W = 0.2898 \text{ MN}$$

$$M_g = 0.2898 * 0.028315 = 8.205 * 10^{-3} \text{ MN-m}$$

$M_g > M_0$, Hence moment under operating condition M_g is controlling, $M_g = M$

Calculation of flange thickness

$$t^2 = M C_F Y / (B S_F), \text{ } S_F \text{ is the allowable stress for the flange material}$$

$$K = A/B = 0.43963/0.325 = 1.3527$$

$$\text{For } K = 1.3527, Y = 10$$

Assuming $C_F = 1$

$$t^2 = 8.205 * 10^{-3} * 1 * 10 / (0.325 * 100)$$

$$t = 0.0502 \text{ m} = 50.2 \text{ mm}$$

$$\text{Actual bolt spacing } B_S = \pi * C / n = (3.14 * 0.40613) / (20) = 0.063 \text{ m}$$

Bolt Pitch Correction Factor

$$C_F = [B_s / (2d+t)]^{0.5} = (0.063 / (2*0.018+0.0502))^{1/2} = 0.855$$

$$\sqrt{C_F} = 0.9246$$

$$\begin{aligned} \text{Actual flange thickness} &= \sqrt{C_F} * t = 0.9246 * 0.063 = 0.04713 \text{ m} \\ &= 0.0464 \text{ m.} \end{aligned}$$

Standard flange thickness available is 50 mm

Channel and channel Cover

$$t_h = G_c \sqrt{(K * P / f)} = 0.345 * \sqrt{(0.3 * 0.33 / 95)} = 0.01114 \text{ m} = 11.14 \text{ mm}$$

$t_h = 14 \text{ mm}$ including corrosion allowance

Tube sheet thickness

$$t_{ts} = F * G \sqrt{(0.25 * P / f)} = 1 * 0.345 * \sqrt{(0.25 * 0.33 / 95)} = 0.0101 \text{ m} = 10.1 \text{ mm}$$

$t_{ts} = 13 \text{ mm}$ including corrosion allowance.

Nozzle design:

1. Tube side Nozzle:

$$\text{Velocity} = V_G = 28 \text{ m/s}$$

$$\text{Area of Nozzle} = (\text{Mass of vapor in}) / (\rho_G * V_G)$$

$$\text{Mass of liquid in} = 2.008 \text{ kg/s}$$

$$\text{Thus, Area of Nozzle} = (2.008) / (2.965 * 28) = 0.024187 \text{ m}^2$$

$$\text{Now, Area of Nozzle} = \pi * d_N^2 / 4 = 0.024187 \text{ m}^2$$

$$d_N^2 = (4 * 0.024187 / \pi)$$

$$d_N = 0.17548 \text{ m} = 17.548 \text{ cm.}$$

2. Shell side Nozzle:

$$\text{Velocity} = V_G = 27 \text{ m/s}$$

$$\text{Area of Nozzle} = (\text{Mass of vapor in}) / (\rho_G * V_G)$$

$$\text{Mass of liquid in} = 2.008 \text{ kg/s}$$

$$\text{Thus, Area of Nozzle} = (2.008) / (3.8 * 27) = 0.01957 \text{ m}^2$$

$$\text{Now, Area of Nozzle} = \pi * d_N^2 / 4 = 0.01957 \text{ m}^2$$

$$d_N^2 = (4 * 0.024187 / \pi)$$

$$d_N = 0.1578 \text{ m} = 15.78 \text{ cm.}$$

Saddle support

Material: low carbon steel

Total length of shell: 4.88 m

Diameter of shell: 325 mm

Knuckle radius: 18.3 mm

Total depth of head (H) = $\sqrt{(D_o r_o / 2)} = \sqrt{(325 * 18.3 / 2)} = 54.53 \text{ mm}$

Density of the steel = 7600 kg/m³.

Weight of steel vessel = 3707.21 kg.

R = D/2 = 162.5 mm

Distance of saddle center line from shell end = A = 0.5R = 81.25 mm

Longitudinal Bending Moment

$$M_1 = QA[1 - (1 - A/L + (R^2 - H^2)/(2AL)) / (1 + 4H/(3L))]$$

$$Q = W/2(L + 4H/3) = 3707.21/2 * (5.88 + 4 * 0.03085/3) = 10975.44 \text{ kg m}$$

$$M_1 = 18.6 \text{ kg-m}$$

Bending moment at center of the span

$$M_2 = QL/4[(1 + 2(R^2 - H^2)/L) / (1 + 4H/(3L)) - 4A/L]$$

$$M_2 = 15706.74 \text{ kg-m.}$$

Stresses in shell at the saddle

(a) At the top most fiber of the cross section

$$f_1 = M_1 / (k_1 \pi R^2 t) \quad k_1 = k_2 = 1$$

$$= 18.6 / (3.14 * 0.1625^2 * 0.01) = 0.02242 \text{ kg/mm}^2$$

Stress in the shell at mid point

$$f_2 = M_2 / (k_2 \pi R^2 t)$$

$$= 9.9656 \text{ kg/mm}^2$$

Axial stress in the shell due to internal pressure

$$f_p = PD/4t$$

$$= 3.4089 \cdot 940 / (4 \cdot 8) = 100.136 \text{ kg/cm}^2 = 1.00136 \text{ kg/mm}^2$$

$$f_2 + f_p = 10.96696 \text{ kg/mm}^2$$

The sum f_2 and f_p is well within the permissible values.